

# Package ‘SBSA’

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**Type** Package

**Title** Simplified Bayesian Sensitivity Analysis

**Version** 0.2.3

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**Description** Simplified Bayesian Sensitivity Analysis

**URL** <http://sbsa.r-forge.r-project.org/>

**License** GPL (>= 3)

**LazyLoad** yes

**Depends** R (>= 3.0.2)

**Imports** Rcpp (>= 0.8.6)

**Suggests** MASS, xtable

**LinkingTo** Rcpp (>= 0.8.6), RcppArmadillo (>= 0.2.6)

**SystemRequirements** GNU make

**NeedsCompilation** yes

**Repository** CRAN

**Date/Publication** 2014-01-31 21:47:18

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SBSA-package	<i>Simplified Bayesian Sensitivity Analysis</i>
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## Description

Simplified Bayesian sensitivity analysis of models with partially observed confounders.

## Details

The SBSA package is an implementation of algorithms for simplified Bayesian sensitivity analysis described in Gustafson *et al* (2010). It has one entry function, [fitSBSA](#). For more details refer to the relevant help files.

## Author(s)

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## References

Gustafson, P., L. C. McCandless, A. R. Levy, and S. Richardson. (2010) ‘Simplified Bayesian Sensitivity Analysis for Mismeasured and Unobserved Confounders.’ *Biometrics*, 66(4):1129-1137.  
DOI: 10.1111/j.1541-0420.2009.01377.x

## See Also

[fitSBSA](#)

## Examples

```
## see examples for fitSBSA
```

fitSBSA	<i>Fitting Simplified Bayesian Sensitivity Models</i>
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## Description

Conducts sensitivity analysis over a model involving unobserved and poorly measured covariates.

## Usage

```
fitSBSA(y, x, w, a, b, k2=NULL, e12=NULL,
        cor.alpha=0, sd.alpha=1e+06, nrep=5000,
        sampler.jump=c(alpha=.15, beta.z=.1, sigma.sq=.5, tau.sq=.05,
                        beta.u.gamma.x=.3, gamma.z=.15),
        q.steps=25, family=c("continuous", "binary"))
```

## Arguments

y	a vector of outcomes
x	a (standardized) vector of exposures
w	a (standardized) matrix of noisy measurements
a	parameter of the prior for magnitude of measurement error on confounder $Z_j$
b	parameter of the prior for magnitude of measurement error on confounder $Z_j$
k2	(optional) magnitude of prior uncertainty about $(U X, Z)$ regression coefficients
e12	(optional) residual variance for $(U X, Z)$
cor.alpha	(optional) value of the $\rho$ parameter of the bivariate normal prior for $\alpha$
sd.alpha	(optional) value of the $\sigma$ parameter of the bivariate normal prior for $\alpha$
nrep	number of MCMC steps
sampler.jump	named vector of standard deviation of <ul style="list-style-type: none"> <li>• alpha jump for block reparametrizing <math>\alpha</math></li> <li>• beta.z jump for block reparametrizing <math>\beta_z</math></li> <li>• sigma.sq (continuous case only) jump for block reparametrizing <math>\sigma^2</math></li> <li>• tau.sq jump for block reparametrizing <math>\tau^2</math></li> <li>• beta.u.gamma.x jump for block reparametrizing <math>\beta_u</math> and <math>\gamma_z</math></li> <li>• gamma.z jump for block reparametrizing <math>\gamma_z</math></li> </ul>
q.steps	number of steps in numeric integration of likelihood (only used for binary outcome variables)
family	a character string indicating the assumed distribution of the outcome. Valid values are "continuous", the default, or "binary".

## Details

The function uses a simplified Bayesian sensitivity analysis algorithm that models the outcome variable  $Y$  in terms of exposure  $X$  and confounders  $Z = (Z_1, \dots, Z_p)$  and  $U = (U_1, \dots, U_q)$ , where  $U$ s are unobserved, and  $Z$ s are measured imprecisely as  $W$ s. (I.e., the observed data is  $(Y, X, W)$ .) Parameters of the model are then estimated using MCMC with reparametrizing block-sampling. The estimated parameters are as follows:

- $\tau: (W|Y, U, Z, X) \sim N_p(Z, \text{diag}(\tau^2))$
- $\gamma_x, \gamma_z: (U|X, Z) \sim N(\gamma_x X + \gamma'_z Z)$
- $\alpha, \beta_u, \beta_z, \sigma: (Y|U, Z, X) \sim N(\alpha_0 + \alpha_x X + \beta_u U + \beta'_z Z, \sigma^2)$

## Value

a list with the following elements:

acc	a vector of counts of how many times each block sampler successfully made a jump. Vector elements are named by their block, as in the <code>sampler.jump</code> argument.
alpha	a $nrep \times 2$ matrix of the value of $\alpha$ parameter at each MCMC step

beta.z	a $nrep \times p$ matrix of the value of $\beta_z$ parameter at each MCMC step
gamma.z	a $nrep \times p$ matrix of the value of $\gamma_z$ parameter at each MCMC step
tau.sq	a $nrep \times p$ matrix of the value of $\tau^2$ parameter at each MCMC step
gamma.x	a vector of the value of $\gamma_x$ parameter at each MCMC step
beta.u	a vector of the value of $\beta_u$ parameter at each MCMC step
sigma.sq	a vector of the value of $\sigma^2$ parameter at each MCMC step

## References

Gustafson, P. and McCandless, L. C and Levy, A. R. and Richardson, S. (2010) *Simplified Bayesian Sensitivity Analysis for Mismeasured and Unobserved Confounders*. Biometrics, 66(4):1129–1137. DOI: 10.1111/j.1541-0420.2009.01377.x

## Examples

```
### simulated data example
n <- 1000

### exposure and true confounders equi-correlated with corr=.6
tmp <- sqrt(.6)*matrix(rnorm(n),n,5) +
      sqrt(1-.6)*matrix(rnorm(n*5),n,5)
x <- tmp[,1]
z <- tmp[,2:5]

### true outcome relationship
y <- rnorm(n, x + z%*%rep(.5,4), .5)

### first two confounders are poorly measured, ICC=.7, .85
### third is correctly measured, fourth is unobserved
w <- z[,1:3]
w[,1] <- w[,1] + rnorm(n, sd=sqrt(1/.7-1))
w[,2] <- w[,2] + rnorm(n, sd=sqrt(1/.85-1))

### fitSBSA expects standardized exposure, noisy confounders
x.sdz <- (x-mean(x))/sqrt(var(x))
w.sdz <- apply(w, 2, function(x) {(x-mean(x)) / sqrt(var(x))} )

### prior information: ICC very likely above .6, mode at .8
### via Beta(5,21) distribution
fit <- fitSBSA(y, x.sdz, w.sdz, a=5, b=21, nrep=10000,
               sampler.jump=c(alpha=.02, beta.z=.03,
                               sigma.sq=.05, tau.sq=.004,
                               beta.u.gamma.x=.4, gamma.z=.5))

### check MCMC behaviour
print(fit$acc)
plot(fit$alpha[,2], pch=20)

### inference on target parameter in original scale
```

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```
trgt <- fit$alpha[1001:10000,2]/sqrt(var(x))
print(c(mean(trgt), sqrt(var(trgt))))
```

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