

Package ‘BRISC’

March 3, 2022

Type Package

Title Fast Inference for Large Spatial Datasets using BRISC

Version 1.0.4

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Depends R (>= 3.3.0), RANN, parallel, stats, rdist, matrixStats,
pbapply, graphics

Description Fits bootstrap with univariate spatial regression models using Bootstrap for Rapid Inference on Spatial Covariances (BRISC) for large datasets using nearest neighbor Gaussian processes detailed in Saha and Datta (2018) <doi:10.1002/sta4.184>.

License GPL (>= 2)

URL <https://github.com/ArkajyotiSaha/BRISC>

BugReports <https://github.com/ArkajyotiSaha/BRISC/issues>

Encoding UTF-8

NeedsCompilation yes

RoxygenNote 6.1.1

Repository CRAN

Date/Publication 2022-03-03 15:40:13 UTC

R topics documented:

BRISC_bootstrap	2
BRISC_correlation	4
BRISC_decorrelation	6
BRISC_estimation	9
BRISC_neighbor	13

BRISC_order	14
BRISC_prediction	16
BRISC_simulation	18
BRISC_variogram.ci	20

Index	22
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BRISC_bootstrap	<i>Function for performing bootstrap with BRISC</i>
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Description

The function `BRISC_bootstrap` performs bootstrap to provide confidence intervals for parameters of univariate spatial regression models using outputs of `BRISC_estimation`. The details of the bootstrap method can be found in BRISC (Saha & Datta, 2018). The optimization is performed with C library of limited-memory BFGS `libLBFGS`: a library of Limited-memory Broyden-Fletcher-Goldfarb-Shanno (L-BFGS), <http://www.chokkan.org/software/liblbfgs/> (Naoaki Okazaki). For user convenience the source codes of the package `libLBFGS` are provided in the package. Some code blocks are borrowed from the R package: `spNNGP`: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes <https://CRAN.R-project.org/package=spNNGP>.

Usage

```
BRISC_bootstrap(BRISC_Out, n_boot = 100, h = 1, n_omp = 1,
               init = "Initial", verbose = TRUE,
               nugget_status = 1)
```

Arguments

<code>BRISC_Out</code>	an object of class <code>BRISC_Out</code> , obtained as an output of <code>BRISC_estimation</code> .
<code>n_boot</code>	number of bootstrap samples. Default value is 100.
<code>h</code>	number of core to be used in parallel computing setup for bootstrap samples. If <code>h = 1</code> , there is no parallelization. Default value is 1.
<code>n_omp</code>	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
<code>init</code>	keyword that specifies initialization scheme to be used. Supported keywords are: "Initial" and "Estimate" for initialization of parameter values for bootstrap samples with initial values used in <code>BRISC_estimate</code> and estimated values of parameters in <code>BRISC_estimate</code> respectively.
<code>verbose</code>	if <code>TRUE</code> , model specifications along with information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is <code>TRUE</code> .
<code>nugget_status</code>	if <code>nugget_status = 0</code> , <code>tau.sq</code> is fixed to 0, if <code>nugget_status = 1</code> <code>tau.sq</code> is estimated. Default value is 1.

Value

A list comprising of the following:

<code>boot.Theta</code>	estimates of spatial covariance parameters corresponding to bootstrap samples.
<code>boot.Beta</code>	estimates of beta corresponding to bootstrap samples.
<code>confidence.interval</code>	confidence intervals corresponding to the parameters.
<code>boot.time</code>	time (in seconds) required to perform the bootstrapping after preprocessing data in R, reported using <code>proc.time()</code> .

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References

- Saha, A., & Datta, A. (2018). BRISC: bootstrap for rapid inference on spatial covariances. *Stat*, e184, DOI: 10.1002/sta4.184.
- Okazaki N. libLBFGS: a library of Limited-memory Broyden-Fletcher-Goldfarb-Shanno (L-BFGS), <http://www.chokkan.org/software/liblbfgs/>.
- Andrew Finley, Abhirup Datta and Sudipto Banerjee (2017). spNNGP: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes. R package version 0.1.1. <https://CRAN.R-project.org/package=spNNGP>

Examples

```
rmvn <- function(n, mu = 0, V = matrix(1)){
  p <- length(mu)
  if(any(is.na(match(dim(V),p))))
    stop("Dimension not right!")
  D <- chol(V)
  t(matrix(rnorm(n*p), ncol=p)%*%D + rep(mu,rep(n,p)))
}

set.seed(1)
n <- 300
coords <- cbind(runif(n,0,1), runif(n,0,1))

beta <- c(1,5)
x <- cbind(rnorm(n), rnorm(n))

sigma.sq = 1
phi = 5
tau.sq = 0.1

B <- as.matrix(beta)
D <- as.matrix(dist(coords))
```

```

R <- exp(-phi*D)
w <- rmv(1, rep(0,n), sigma.sq*R)

y <- rnorm(n, x%%B + w, sqrt(tau.sq))

estimation_result <- BRISC_estimation(coords, y, x)
bootstrap_result <- BRISC_bootstrap(estimation_result, n_boot = 10)

```

BRISC_correlation *Function for simulating correlated data with BRISC*

Description

The function `BRISC_correlation` creates correlated data (known structure) using Nearest Neighbor Gaussian Processes (NNGP). `BRISC_correlation` uses the sparse Cholesky representation of Vecchia's likelihood developed in Datta et al., 2016. Some code blocks are borrowed from the R package: `spNNGP`: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes <https://CRAN.R-project.org/package=spNNGP> .

Usage

```

BRISC_correlation(coords, sim, sigma.sq = 1, tau.sq = 0, phi = 1,
                  nu = 1.5, n.neighbors = NULL, n_omp = 1,
                  cov.model = "exponential",
                  search.type = "tree", stabilization = NULL,
                  verbose = TRUE, tol = 12)

```

Arguments

<code>coords</code>	an $n \times 2$ matrix of the observation coordinates in R^2 (e.g., easting and northing).
<code>sim</code>	an $n \times k$ matrix of the k many $n \times 1$ vectors from which the correlated data are calculated (see Details below).
<code>sigma.sq</code>	value of sigma square. Default value is 1.
<code>tau.sq</code>	value of tau square. Default value is 0.1.
<code>phi</code>	value of phi. Default value is 1.
<code>nu</code>	value of nu, only required for matern covariance model. Default value is 1.5.
<code>n.neighbors</code>	number of neighbors used in the NNGP. Default value is $\max(100, n - 1)$. We suggest a high value of <code>n.neighbors</code> for lower value of <code>phi</code> .
<code>n_omp</code>	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
<code>cov.model</code>	keyword that specifies the covariance function to be used in modelling the spatial dependence structure among the observations. Supported keywords are: "exponential", "matern", "spherical", and "gaussian" for exponential, Matern, spherical and Gaussian covariance function respectively. Default value is "exponential".

search.type	keyword that specifies type of nearest neighbor search algorithm to be used. Supported keywords are: "brute", "tree" and "cb". "brute" and "tree" provide the same result, though "tree" should be faster. "cb" implements fast code book search described in Ra and Kim (1993) modified for NNGP. If locations do not have identical coordinate values on the axis used for the nearest neighbor determination, then "cb" and "brute" should produce identical neighbor sets. However, if there are identical coordinate values on the axis used for nearest neighbor determination, then "cb" and "brute" might produce different, but equally valid neighbor sets, e.g., if data are on a grid. Default value is "tree".
stabilization	when we use a very smooth covarince model (lower values of phi for spherical and Gaussian covariance and low phi and high nu for Matern covarince) in absence of a non-negligible nugget, the correlation process may fail due to computational instability. If stabilization = TRUE, performs stabilization by setting $\tau.sq = \max\tau.sq, \sigma.sq * 1e - 06$. Default value is TRUE for cov.model = "exponential" and FALSE otherwise.
verbose	if TRUE, model specifications along with information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is TRUE.
tol	the input observation coordinates are rounded to this many places after the decimal. The default value is 12.

Details

Denote g be the input `sim`. Let Σ be the precision matrix associated with the covariance model determined by the `cov.model` and model parameters. Then BRISC_correlation calculates h , where h is given as follows:

$$S^{-0.5}h = g$$

where, $S^{-0.5}$ is a sparse approximation of the cholesky factor $\Sigma^{-0.5}$ of the precision matrix Σ^{-1} , obtained from NNGP.

Value

A list comprising of the following:

coords	the matrix coords.
n.neighbors	the used value of n.neighbors.
cov.model	the used covariance model.
Theta	parameters of covarince model; accounts for stabilization.
input.data	the matrix <code>sim</code> .
output.data	the output matrix h in Details.
time	time (in seconds) required after preprocessing data in R, reported using <code>proc.time()</code> .

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References

Datta, A., S. Banerjee, A.O. Finley, and A.E. Gelfand. (2016) Hierarchical Nearest-Neighbor Gaussian process models for large geostatistical datasets. *Journal of the American Statistical Association*, 111:800-812.

Andrew Finley, Abhirup Datta and Sudipto Banerjee (2017). *spNNGP: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes*. R package version 0.1.1. <https://CRAN.R-project.org/package=spNNGP>

Examples

```
set.seed(1)
n <- 1000
coords <- cbind(runif(n,0,1), runif(n,0,1))

sigma.sq = 1
phi = 1

set.seed(1)
sim <- matrix(rnorm(3*n),n, 3)
correlation_result <- BRISC_correlation(coords, sigma.sq = sigma.sq,
                                       phi = phi, sim = sim)
```

BRISC_decorrelation *Function for decorrelating data with BRISC*

Description

The function `BRISC_decorrelation` is used to decorrelate data (known structure) using Nearest Neighbor Gaussian Processes (NNGP). `BRISC_decorrelation` uses the sparse Cholesky representation of Vecchia's likelihood developed in Datta et al., 2016. Some code blocks are borrowed from the R package: `spNNGP: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes` <https://CRAN.R-project.org/package=spNNGP> .

Usage

```
BRISC_decorrelation(coords, sim, sigma.sq = 1, tau.sq = 0,
                   phi = 1, nu = 1.5, n.neighbors = NULL,
                   n_omp = 1, cov.model = "exponential",
                   search.type = "tree",
                   stabilization = NULL, verbose = TRUE,
                   tol = 12)
```

Arguments

<code>coords</code>	an $n \times 2$ matrix of the observation coordinates in R^2 (e.g., easting and northing).
<code>sim</code>	an $n \times k$ matrix of the k many $n \times 1$ vectors from which the decorrelated data are calculated (see Details below).
<code>sigma.sq</code>	value of sigma square. Default value is 1.
<code>tau.sq</code>	value of tau square. Default value is 0.1.
<code>phi</code>	value of phi. Default value is 1.
<code>nu</code>	value of nu, only required for Matern covariance model. Default value is 1.5.
<code>n.neighbors</code>	number of neighbors used in the NNGP. Default value is $\max(100, n - 1)$. We suggest a high value of <code>n.neighbors</code> for lower value of <code>phi</code> .
<code>n_omp</code>	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
<code>cov.model</code>	keyword that specifies the covariance function to be used in modelling the spatial dependence structure among the observations. Supported keywords are: "exponential", "matern", "spherical", and "gaussian" for exponential, Matern, spherical and Gaussian covariance function respectively. Default value is "exponential".
<code>search.type</code>	keyword that specifies type of nearest neighbor search algorithm to be used. Supported keywords are: "brute", "tree" and "cb". "brute" and "tree" provide the same result, though "tree" should be faster. "cb" implements fast code book search described in Ra and Kim (1993) modified for NNGP. If locations do not have identical coordinate values on the axis used for the nearest neighbor determination, then "cb" and "brute" should produce identical neighbor sets. However, if there are identical coordinate values on the axis used for nearest neighbor determination, then "cb" and "brute" might produce different, but equally valid neighbor sets, e.g., if data are on a grid. Default value is "tree".
<code>stabilization</code>	when the correlated data are generated from a very smooth covariance model (lower values of phi for spherical and Gaussian covariance and low phi and high nu for Matern covariance), the decorrelation process may fail due to computational instability. If <code>stabilization = TRUE</code> , performs stabilization by adding a white noise to the data with <code>nugget tau.sq = sigma.sq * 1e-06</code> . Default value is TRUE for <code>cov.model = "exponential"</code> and FALSE otherwise.
<code>verbose</code>	if TRUE, model specifications along with information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is TRUE.
<code>tol</code>	the input observation coordinates are rounded to this many places after the decimal. The default value is 12.

Details

Denote h be the input `sim`. Let Σ be the covariance matrix associated with the covariance model determined by the `cov.model` and model parameters. Then BRISC_decorrelation calculates g , where g is given as follows:

$$S^{-0.5}h = g$$

where, $S^{-0.5}$ is a sparse approximation of the cholesky factor $\Sigma^{-0.5}$ of the precision matrix Σ^{-1} , obtained from NNGP.

Value

A list comprising of the following:

<code>coords</code>	the matrix <code>coords</code> .
<code>n.neighbors</code>	the used value of <code>n.neighbors</code> .
<code>cov.model</code>	the used covariance model.
<code>Theta</code>	parameters of covarinace model; accounts for stabilization.
<code>input.data</code>	if <code>stabilization = FALSE</code> , return the matrix <code>sim</code> . If <code>stabilization = TRUE</code> , returns <code>sim + used white noise in stabilization process</code> .
<code>output.data</code>	the output matrix g in Details.
<code>time</code>	time (in seconds) required after preprocessing data in R, reported using, <code>proc.time()</code> .

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References

Datta, A., S. Banerjee, A.O. Finley, and A.E. Gelfand. (2016) Hierarchical Nearest-Neighbor Gaussian process models for large geostatistical datasets. *Journal of the American Statistical Association*, 111:800-812.

Andrew Finley, Abhirup Datta and Sudipto Banerjee (2017). `spNNGP`: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes. R package version 0.1.1. <https://CRAN.R-project.org/package=spNNGP>

Examples

```
rmvn <- function(n, mu = 0, V = matrix(1)){
  p <- length(mu)
  if(any(is.na(match(dim(V),p))))
    stop("Dimension not right!")
  D <- chol(V)
  t(matrix(rnorm(n*p), ncol=p)%*%D + rep(mu,rep(n,p)))
}

set.seed(1)
n <- 1000
coords <- cbind(runif(n,0,1), runif(n,0,1))

sigma.sq = 1
phi = 1

set.seed(1)
```



```
D <- as.matrix(dist(coords))
R <- exp(-phi*D)
sim <- rmvn(3, rep(0,n), sigma.sq*R)
decorrelation_result <- BRISC_decorrelation(coords, sim = sim)
```

BRISC_estimation *Function for estimation with BRISC*

Description

The function `BRISC_estimation` fits univariate spatial regression models for large spatial data using Vecchia's approximate likelihood (Vecchia, 1988). `BRISC_estimation` uses the sparse Cholesky representation of Vecchia's likelihood developed in Datta et al., 2016. The Maximum Likelihood Estimates (MLE) of the parameters are used later for calculating the confidence interval via the `BRISC_bootstrap` (BRISC, Saha & Datta, 2018).

We recommend using `BRISC_estimation` followed by `BRISC_bootstrap` to obtain the confidence intervals for the model parameters.

The optimization is performed with C library of limited-memory BFGS `libLBFGS`: a library of Limited-memory Broyden-Fletcher-Goldfarb-Shanno (L-BFGS), <http://www.chokkan.org/software/liblbfgs/> (Naoaki Okazaki). For user convenience the source codes of the package `libLBFGS` are provided in the package. The code for the coordinate ordering method, approximate Maximum Minimum Distance (Guinness, 2018) is available in https://github.com/joeguinness/gp_reorder/tree/master/R and is adopted with minor modification. Some code blocks are borrowed from the R package: `spNNGP`: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes <https://CRAN.R-project.org/package=spNNGP>.

Usage

```
BRISC_estimation(coords, y, x = NULL, sigma.sq = 1,
                 tau.sq = 0.1, phi = 1,
                 nu = 1.5, n.neighbors = 15,
                 n_omp = 1, order = "Sum_coords",
                 cov.model = "exponential",
                 search.type = "tree",
                 stabilization = NULL,
                 pred.stabilization = 1e-8,
                 verbose = TRUE, eps = 2e-05,
                 nugget_status = 1, ordering = NULL,
                 neighbor = NULL, tol = 12)
```

Arguments

<code>coords</code>	an $n \times 2$ matrix of the observation coordinates in R^2 (e.g., easting and northing).
<code>y</code>	an n length vector of response at the observed coordinates.
<code>x</code>	an $n \times p$ matrix of the covariates in the observation coordinates. Default value is $n \times 1$ matrix of 1 to adjust for the mean(intercept).

<code>sigma.sq</code>	starting value of sigma square. Default value is 1.
<code>tau.sq</code>	starting value of tau square. Default value is 0.1.
<code>phi</code>	starting value of phi. Default value is 1.
<code>nu</code>	starting value of nu, only required for matern covariance model. Default value is 1.5.
<code>n.neighbors</code>	number of neighbors used in the NNGP. Default value is 15.
<code>n_omp</code>	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
<code>order</code>	keyword that specifies the ordering scheme to be used in ordering the observations. Supported keywords are: "AMMD" and "Sum_coords" for approximate Maximum Minimum Distance and sum of coordinate based ordering, respectively. Default value is "Sum_coords". $n > 65$ is required for "AMMD". Ignored, if "ordering" is not NULL.
<code>cov.model</code>	keyword that specifies the covariance function to be used in modelling the spatial dependence structure among the observations. Supported keywords are: "exponential", "matern", "spherical", and "gaussian" for exponential, Matern, spherical and Gaussian covariance function respectively. Default value is "exponential".
<code>search.type</code>	keyword that specifies type of nearest neighbor search algorithm to be used. Supported keywords are: "brute", "tree" and "cb". "brute" and "tree" provide the same result, though "tree" should be faster. "cb" implements fast code book search described in Ra and Kim (1993) modified for NNGP. If locations do not have identical coordinate values on the axis used for the nearest neighbor ordering (see <code>order</code> argument) then "cb" and "brute" should produce identical neighbor sets. However, if there are identical coordinate values on the axis used for nearest neighbor ordering, then "cb" and "brute" might produce different, but equally valid, neighbor sets, e.g., if data are on a grid. Default value is "tree". Ignored, if "neighbor" is not NULL.
<code>stabilization</code>	when the spatial errors are generated from a very smooth covariance model (lower values of phi for spherical and Gaussian covariance and low phi and high nu for Matern covariance), the estimation process may fail due to computational instability. If <code>stabilization = TRUE</code> , performs stabilization by adding a white noise to the reordered data with <code>nugget tau.sq = sigma.sq * 1e-06</code> . Estimation is performed on this new data with <code>nugget_status = 1</code> (see <code>nugget_status</code> argument below). Default value is TRUE for <code>cov.model = "exponential"</code> and FALSE otherwise.
<code>pred.stabilization</code>	if not NULL, will truncate the estimated tau square to <code>pred.stabilization * estimated sigma square</code> . This provides additional stability in BRISC_prediction. Default value is $1e - 8$.
<code>verbose</code>	if TRUE, model specifications along with information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is TRUE.
<code>eps</code>	tolerance to be used in centred finite difference approximation of derivatives. Default value is $2e-05$.

nugget_status	if nugget_status = 0, tau.sq is fixed to 0, if nugget_status = 1 tau.sq is estimated. Default value is 1.
ordering	if NULL, the observed locations will be ordered following the scheme in "order". If not NULL, the ordering step is bypassed and the input must denote the n length integer vector of ordering of the input coordinates that is to be used as the ordering of the coordinates for determination of the set of nearest neighbors. Output from BRISC_order can be used here.
neighbor	if NULL, neighbor set and corresponding information are created using the search type specified in "search.type". If not NULL, the step of searching the neighbors is bypassed and the input must be an output from BRISC_neighbor with identical input in "order", "ordering" and "search.type".
tol	the input observation coordinates, response and the covariates are rounded to this many places after the decimal. The default value is 12.

Value

An object of class BRISC_Out, which is a list comprising:

ord	the vector of indices used to order data necessary for fitting the NNGP model.
coords	the matrix coords[ord,].
y	If stabilization = FALSE, returns the vector y[ord]. If stabilization = TRUE, returns y[ord] + used white noise in stabilization process.
X	the matrix x[ord, ,drop=FALSE].
n.neighbors	the used value of n.neighbors.
cov.model	the used covariance model.
eps	value of used eps for approximate derivation. Default value is 2e-05.
init	initial values of the parameters of the covariance model; accounts for stabilization.
Beta	estimate of beta.
Theta	estimate of parameters of covarinace model.
log_likelihood	value of Vecchia's approximate log likelihood with parameter estimates.
estimation.time	time (in seconds) required to perform the model fitting after ordering and pre-processing data in R, reported using proc.time().
BRISC_Object	object required for bootstrap and prediction.

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References

- Saha, A., & Datta, A. (2018). BRISC: bootstrap for rapid inference on spatial covariances. *Stat*, e184, DOI: 10.1002/sta4.184.
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- Andrew Finley, Abhirup Datta and Sudipto Banerjee (2020). spNNGP: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes. R package version 0.1.4. <https://CRAN.R-project.org/package=spNNGP>
- Ra, S. W., & Kim, J. K. (1993). A fast mean-distance-ordered partial codebook search algorithm for image vector quantization. *IEEE Transactions on Circuits and Systems II: Analog and Digital Signal Processing*, 40(9), 576-579.

Examples

```
rmvn <- function(n, mu = 0, V = matrix(1)){
  p <- length(mu)
  if(any(is.na(match(dim(V),p))))
    stop("Dimension not right!")
  D <- chol(V)
  t(matrix(rnorm(n*p), ncol=p)%*%D + rep(mu,rep(n,p)))
}

set.seed(1)
n <- 1000
coords <- cbind(runif(n,0,1), runif(n,0,1))

beta <- c(1,5)
x <- cbind(rnorm(n), rnorm(n))

sigma.sq = 1
phi = 1
tau.sq = 0.1

B <- as.matrix(beta)
D <- as.matrix(dist(coords))
R <- exp(-phi*D)
w <- rmvn(1, rep(0,n), sigma.sq*R)

y <- rnorm(n, x%*%B + w, sqrt(tau.sq))
```

```
estimation_result <- BRISC_estimation(coords, y, x)
estimation_result$Theta ##Estimates of covariance model parameters.
estimation_result$Beta ##Estimates of Beta
```

BRISC_neighbor

Function for finding set of nearest neighbors for BRISC

Description

The function BRISC_neighbor creates the set of nearest neighbors for a given set of coordinates, which can be used as an input for "neighbor" argument in BRISC_estimation. This is especially useful for avoiding often computationally intensive nearest neighbor finding scheme in case of multiple application of BRISC_estimation on a fixed set of coordinates.

Usage

```
BRISC_neighbor(coords, n.neighbors = 15, n_omp = 1,
               order = "Sum_coords", search.type = "tree",
               verbose = TRUE, ordering = NULL, tol = 12
               )
```

Arguments

coords	an $n \times 2$ matrix of the observation coordinates in R^2 (e.g., easting and northing).
n.neighbors	number of neighbors used in the NNGP. Default value is 15.
n_omp	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
order	keyword that specifies the ordering scheme to be used in ordering the observations. Supported keywords are: "AMMD" and "Sum_coords" for approximate Maximum Minimum Distance and sum of coordinate based ordering, respectively. Default value is "Sum_coords". $n > 65$ is required for "AMMD". Ignored, if ordering is not NULL.
search.type	keyword that specifies type of nearest neighbor search algorithm to be used. Supported keywords are: "brute", "tree" and "cb". "brute" and "tree" provide the same result, though "tree" should be faster. "cb" implements fast code book search described in Ra and Kim (1993) modified for NNGP. If locations do not have identical coordinate values on the axis used for the nearest neighbor ordering (see order argument) then "cb" and "brute" should produce identical neighbor sets. However, if there are identical coordinate values on the axis used for nearest neighbor ordering, then "cb" and "brute" might produce different, but equally valid, neighbor sets, e.g., if data are on a grid. Default value is "tree".
verbose	if TRUE, information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is TRUE.

ordering	if not NULL, denotes the n length integer vector of ordering of the input coordinates and is used as the ordering of the coordinates for determination of the set of nearest neighbors.
tol	the input observation coordinates, response and the covariates are rounded to this many places after the decimal. The default value is 12.

Value

A list containing information regarding nearest neighbors which can be used as an input for "neighbor" argument in BRISC_estimation.

Author(s)

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References

Saha, A., & Datta, A. (2018). BRISC: bootstrap for rapid inference on spatial covariances. *Stat*, e184, DOI: 10.1002/sta4.184.

Datta, A., S. Banerjee, A.O. Finley, and A.E. Gelfand. (2016) Hierarchical Nearest-Neighbor Gaussian process models for large geostatistical datasets. *Journal of the American Statistical Association*, 111:800-812.

Guinness, J. (2018) Permutation and Grouping Methods for Sharpening Gaussian Process Approximations, *Technometrics*, DOI: 10.1080/00401706.2018.1437476, https://github.com/joeguinness/gp_reorder/tree/master/R .

Examples

```
set.seed(1)
n <- 1000
coords <- cbind(runif(n,0,1), runif(n,0,1))

ordering_result <- BRISC_order(coords)
```

BRISC_order

Function for ordering coordinates with BRISC

Description

The function BRISC_order outputs the ordering for a set of coordinates, which can be used as an input for "ordering" argument in BRISC_estimation. This is especially useful for avoiding often computationally intensive location ordering scheme in case of multiple application of BRISC_estimation on a fixed set of coordinates.

Usage

```
BRISC_order(coords, order = "Sum_coords", verbose = TRUE)
```

Arguments

coords	an $n \times 2$ matrix of the observation coordinates in R^2 (e.g., easting and northing).
order	keyword that specifies the ordering scheme to be used in ordering the observations. Supported keywords are: "AMMD" and "Sum_coords" for approximate Maximum Minimum Distance and sum of coordinate based ordering, respectively. Default value is "Sum_coords". $n > 65$ is required for "AMMD".
verbose	if TRUE, progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is TRUE.

Value

An integer vector of ordering of the input coordinates which can be used as an input for "ordering" argument in BRISC_estimation.

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References

Saha, A., & Datta, A. (2018). BRISC: bootstrap for rapid inference on spatial covariances. *Stat*, e184, DOI: 10.1002/sta4.184.

Datta, A., S. Banerjee, A.O. Finley, and A.E. Gelfand. (2016) Hierarchical Nearest-Neighbor Gaussian process models for large geostatistical datasets. *Journal of the American Statistical Association*, 111:800-812.

Guinness, J. (2018) Permutation and Grouping Methods for Sharpening Gaussian Process Approximations, *Technometrics*, DOI: 10.1080/00401706.2018.1437476, https://github.com/joeguinness/gp_reorder/tree/master/R .

Examples

```
set.seed(1)
n <- 1000
coords <- cbind(runif(n,0,1), runif(n,0,1))

ordering_result <- BRISC_order(coords)
```

BRISC_prediction *Function for performing prediction with BRISC*

Description

The function `BRISC_prediction` performs fast prediction on a set of new locations with univariate spatial regression models using Nearest Neighbor Gaussian Processes (NNGP) (Datta et al., 2016). `BRISC_prediction` uses the parameter estimates from `BRISC_estimation` for the prediction. Some code blocks are borrowed from the R package: `spNNGP: Spatial Regression Models for Large Datasets using Nearest Neighbor Gaussian Processes` <https://CRAN.R-project.org/package=spNNGP> .

Usage

```
BRISC_prediction(BRISC_Out, coords.0, X.0 = NULL, n_omp = 1,
                 verbose = TRUE, tol = 12)
```

Arguments

<code>BRISC_Out</code>	an object of class <code>BRISC_Out</code> , obtained as an output of <code>BRISC_estimation</code> .
<code>coords.0</code>	the spatial coordinates corresponding to prediction locations. Its structure should be same as that of <code>coords</code> in <code>BRISC_estimation</code> . Default value is a column of 1 to adjust for the mean (intercept).
<code>X.0</code>	the covariates for prediction locations. Its Structure should be identical (including intercept) with that of covariates provided for estimation purpose in <code>BRISC_estimation</code> .
<code>n_omp</code>	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
<code>verbose</code>	if <code>TRUE</code> , model specifications along with information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is <code>TRUE</code> .
<code>tol</code>	the coordinates and the covariates corresponding to the prediction locations are rounded to this many places after the decimal. The default value is 12.

Value

A list comprising of the following:

<code>prediction</code>	predicted response corresponding to <code>X.0</code> and <code>coords.0</code> .
<code>prediction.ci</code>	confidence intervals corresponding to the predictions.
<code>prediction.time</code>	time (in seconds) required to perform the prediction after preprocessing data in R, reported using <code>proc.time()</code> .

BRISC_simulation *Function to simulate data with BRISC*

Description

The function `BRISC_simulation` simulates correlated data (known structure) using Nearest Neighbor Gaussian Processes (NNGP). `BRISC_simulation` uses the sparse Cholesky representation of Vecchia's likelihood developed in Datta et al., 2016. `BRISC_simulation` uses [BRISC_correlation](#) for this purpose.

Usage

```
BRISC_simulation(coords, sim_number = 1,
                 seeds = NULL, sigma.sq = 1,
                 tau.sq = 0, phi = 1, nu = 1.5,
                 n.neighbors = NULL, n_omp = 1,
                 cov.model = "exponential",
                 search.type = "tree",
                 stabilization = NULL,
                 verbose = TRUE, tol = 12)
```

Arguments

<code>coords</code>	an $n \times 2$ matrix of the observation coordinates in R^2 (e.g., easting and northing).
<code>sim_number</code>	number of simulations. Default value is 1.
<code>seeds</code>	seeds which are used in generation of the initial independent data. Default value is NULL. If non-null, the number of seeds must be equal to <code>sim_number</code> .
<code>sigma.sq</code>	value of sigma square. Default value is 1.
<code>tau.sq</code>	value of tau square. Default value is 0.1.
<code>phi</code>	value of phi. Default value is 1.
<code>nu</code>	starting value of nu, only required for matern covariance model. Default value is 1.5.
<code>n.neighbors</code>	number of neighbors used in the NNGP. Default value is 15.
<code>n_omp</code>	number of threads to be used, value can be more than 1 if source code is compiled with OpenMP support. Default is 1.
<code>cov.model</code>	keyword that specifies the covariance function to be used in modelling the spatial dependence structure among the observations. Supported keywords are: "exponential", "matern", "spherical", and "gaussian" for exponential, Matern, spherical and Gaussian covariance function respectively. Default value is "exponential".
<code>search.type</code>	keyword that specifies type of nearest neighbor search algorithm to be used. Supported keywords are: "brute", "tree" and "cb". "brute" and "tree" provide the same result, though "tree" should be faster.

"cb" implements fast code book search described in Ra and Kim (1993) modified for NNGP. If locations do not have identical coordinate values on the axis used for the nearest neighbor ordering (see order argument) then "cb" and "brute" should produce identical neighbor sets. However, if there are identical coordinate values on the axis used for nearest neighbor ordering, then "cb" and "brute" might produce different, but equally valid, neighbor sets, e.g., if data are on a grid. Default value is "tree".

stabilization	when we use a very smooth covarince model (lower values of phi for spherical and Gaussian covariance and low phi and high nu for Matern covarince) in absence of a non-negligible nugget, the correlation process may fail due to computational instability. If stabilization = TRUE, performs stabilization by setting $\tau.sq = \max\tau.sq, \sigma.sq * 1e - 06$. Default value is TRUE for cov.model = "exponential" and FALSE otherwise.
verbose	if TRUE, model specifications along with information regarding OpenMP support and progress of the algorithm is printed to the screen. Otherwise, nothing is printed to the screen. Default value is TRUE.
tol	the input observation coordinates are rounded to this many places after the decimal. The default value is 12.

Value

A list comprising of the following:

coords	the matrix coords.
n.neighbors	the used value of n.neighbors.
cov.model	the used covariance model.
Theta	parameters of covarince model; accounts for stabilization.
input.data	the $n \times sim_number$ matrix of generated independent data. Here i^{th} column denotes the data corresponding to the i^{th} simulation.
output.data	the $n \times sim_number$ matrix of generated correlated data. Here i^{th} column denotes the data corresponding to the i^{th} simulation.
time	time (in seconds) required after preprocessing data in R, reported using, <code>proc.time()</code> .

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Examples

```
set.seed(1)
n <- 1000
coords <- cbind(runif(n,0,1), runif(n,0,1))

sigma.sq = 1
```

```
phi = 1  
simulation_result <- BRISC_simulation(coords, sim_number = 3)
```

BRISC_variogram.ci *Function for plotting estimated Variogram and confidence region*

Description

The function BRISC_variogram.ci plots estimated Variogram and associated confidence region. BRISC_variogram.ci uses the parameter estimates from BRISC_estimation and associated confidence interval from BRISC_bootstrap.

Usage

```
BRISC_variogram.ci(BRISC_Out, confidence_est,  
                  plot.variogram = FALSE)
```

Arguments

BRISC_Out an object of class BRISC_Out, obtained as an output of BRISC_estimation.

confidence_est bootstrap sample of the Theta parameters, obtained from BRISC_bootstrap.

plot.variogram if TRUE, plots the variogram and the associated confidence region. Default is FALSE.

Value

A list comprising of the following:

variogram variogram and associated confidence region corresponding to lag ranging from 0 to 20, evaluated at 0.01 frequency.

Plot plots the Variogram and associated confidence region with legends.

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Examples

```

rmvn <- function(n, mu = 0, V = matrix(1)){
  p <- length(mu)
  if(any(is.na(match(dim(V),p))))
    stop("Dimension not right!")
  D <- chol(V)
  t(matrix(rnorm(n*p), ncol=p)%*%D + rep(mu,rep(n,p)))
}

set.seed(1)
n <- 300
coords <- cbind(runif(n,0,1), runif(n,0,1))

beta <- c(1,5)
x <- cbind(rnorm(n), rnorm(n))

sigma.sq = 1
phi = 5
tau.sq = 0.1

B <- as.matrix(beta)
D <- as.matrix(dist(coords))
R <- exp(-phi*D)
w <- rmvn(1, rep(0,n), sigma.sq*R)

y <- rnorm(n, x%*%B + w, sqrt(tau.sq))

estimation_result <- BRISC_estimation(coords, y, x)
bootstrap_result <- BRISC_bootstrap(estimation_result, n_boot = 10)
varg <- BRISC_variogram.ci(estimation_result,
                           bootstrap_result$boot.Theta,
                           plot.variogram = TRUE)

```

Index

* **model**

- BRISC_bootstrap, [2](#)
- BRISC_correlation, [4](#)
- BRISC_decorrelation, [6](#)
- BRISC_estimation, [9](#)
- BRISC_neighbor, [13](#)
- BRISC_order, [14](#)
- BRISC_prediction, [16](#)
- BRISC_simulation, [18](#)
- BRISC_variogram.ci, [20](#)

- BRISC_bootstrap, [2](#)
- BRISC_correlation, [4](#), [18](#)
- BRISC_decorrelation, [6](#)
- BRISC_estimation, [9](#)
- BRISC_neighbor, [13](#)
- BRISC_order, [14](#)
- BRISC_prediction, [16](#)
- BRISC_simulation, [18](#)
- BRISC_variogram.ci, [20](#)