

# Package ‘varycoef’

June 3, 2021

**Type** Package

**Title** Modeling Spatially Varying Coefficients

**Version** 0.3.1

**Description** Implements a maximum likelihood estimation (MLE) method for estimation and prediction of Gaussian process-based spatially varying coefficient (SVC) models (Dambon et al. (2021a) <[doi:10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470)>). Covariance tapering (Furrer et al. (2006) <[doi:10.1198/106186006X132178](https://doi.org/10.1198/106186006X132178)>) can be applied such that the method scales to large data. Further, it implements a joint variable selection of the fixed and random effects (Dambon et al. (2021b) <[arXiv:2101.01932](https://arxiv.org/abs/2101.01932)>).

**License** GPL-2

**URL** <https://github.com/jakobdambon/varycoef>

**BugReports** <https://github.com/jakobdambon/varycoef/issues>

**Depends** R (>= 3.5.0), spam

**Imports** glmnet, lhs, mlr, mlrMBO, RandomFields, optimParallel (>= 0.8-1), ParamHelpers, pbapply, smooof, sp

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check_cov_lower	<i>Check Lower Bound of Covariance Parameters</i>
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### Description

Ensures that the covariance parameters define a positive definite covariance matrix. It takes the vector  $(\rho_1, \sigma_1^2, \dots, \rho_q, \sigma_q^2, \tau^2)$  and checks if all  $\rho_k > 0$ , all  $\sigma_k^2 \geq 0$ , and  $\tau^2 > 0$ .

### Usage

```
check_cov_lower(cv, q)
```

**Arguments**

cv                   (numeric(2\*q+1))  
Covariance vector of SVC model.

q                    (numeric(1))  
Integer indicating the number of SVCs.

**Value**

logical(1) with TRUE if all conditions above are fulfilled.

**Examples**

```
# first one is true, all other are false
check_cov_lower(c(0.1, 0, 0.2, 1, 0.2), q = 2)
check_cov_lower(c(0, 0, 0.2, 1, 0.2), q = 2)
check_cov_lower(c(0.1, 0, 0.2, 1, 0), q = 2)
check_cov_lower(c(0.1, 0, 0.2, -1, 0), q = 2)
```

---

coef.SVC\_mle

*Extract Mean Effects*


---

**Description**

Method to extract the mean effects from an [SVC\\_mle](#) or [SVC\\_selection](#) object.

**Usage**

```
## S3 method for class 'SVC_mle'
coef(object, ...)

## S3 method for class 'SVC_selection'
coef(object, ...)
```

**Arguments**

object               [SVC\\_mle](#) or [SVC\\_selection](#) object

...                   further arguments

**Value**

named vector with mean effects, i.e.  $\mu$  from [SVC\\_mle](#)

**Author(s)**

Jakob Dambon

---

cov_par	<i>Extact Covariance Parameters Function to extract the covariance parameters from an <a href="#">SVC_mle</a> or <a href="#">SVC_selection</a> object.</i>
---------	--

---

### Description

Extact Covariance Parameters

Function to extract the covariance parameters from an [SVC\\_mle](#) or [SVC\\_selection](#) object.

### Usage

```
cov_par(...)
```

```
## S3 method for class 'SVC_mle'
```

```
cov_par(object, ...)
```

```
## S3 method for class 'SVC_selection'
```

```
cov_par(object, ...)
```

### Arguments

...	further arguments
object	<a href="#">SVC_mle</a> or <a href="#">SVC_selection</a> object

### Value

vector with covariance parameters with the following attributes:

- "GRF", character, describing the covariance function used for the GP, see [SVC\\_mle\\_control](#).
- "tapering", either NULL if no tapering is applied of the taper range.

### Author(s)

Jakob Dambon

---

fitted.SVC_mle	<i>Extact Model Fitted Values</i>
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---

### Description

Method to extract the fitted values from an [SVC\\_mle](#) object. This is only possible if `save.fitted` was set to TRUE in the control of the function call

**Usage**

```
## S3 method for class 'SVC_mle'
fitted(object, ...)
```

**Arguments**

```
object      SVC_mle object
...         further arguments
```

**Value**

Data frame, fitted values to given data, i.e., the SVC as well as the response and their locations

**Author(s)**

Jakob Dambon

---

fullSVC_line	<i>Sample Function for GP-based SVC Model on Real Line</i>
--------------	--

---

**Description**

Samples SVC data on a real line. The SVCs parameters and the sample locations have to be provided. The SVCs are assumed to have an Matern covariance function. The sampled model matrix contains an intercept as a first column and further covariates sampled from a standard normal. The SVCs are sampled according to their given parametrization and at respective observation locations. The error vector sampled from a nugget effect. Finally, the response vector is computed.

**Usage**

```
fullSVC_line(df.pars, nugget.sd, locs)
```

**Arguments**

```
df.pars      (data.frame(p, 3))
              Contains the mean and covariance parameters of SVCs. The four columns must
              have the names "mean", "nu", "var", and "scale".

nugget.sd    (numeric(1))
              Standard deviation of the nugget / error term.

locs        (numeric(n))
              The vector contains the observation locations and therefore defines the number
              of observations to be n.
```

**Value**

list

Returns a list with the response  $y$ , model matrix  $X$ , a matrix beta containing the sampled SVC at given locations, a vector eps containing the error, and a vector locs containing the original locations.

**Examples**

```
set.seed(123)
# SVC parameters
(df.pars <- data.frame(
  nu = c(1.5, 1.5),
  var = c(2, 1),
  scale = c(3, 1),
  mean = c(1, 2)))
# nugget standard deviation
tau <- 0.5

# sample locations
s <- sort(runif(500, min = 0, max = 10))
SVCdata <- fullSVC_line(
  df.pars = df.pars,
  nugget.sd = tau,
  locs = s
)
```

---

fullSVC\_reggrid

*Sample Function for GP-based SVC Models on Regular Grid*


---

**Description**

Samples SVC data on a regular quadratic (Cartesian) grid. The SVCs have all mean 0 and an Matern covariance function is used.

**Usage**

```
fullSVC_reggrid(m, p, cov_pars, nugget, seed = 123, given.locs = NULL)
```

**Arguments**

m	(numeric(1)) Number of observations in one dimension, i.i, the square root number of total number of observation locations $n = m^2$ .
p	(numeric(1)) Number of SVCs.

cov_pars	(data.frame(p,2)) Contains the covariance parameters of SVCs. The two columns must have the names "nu", "var" and "scale". These covariance parameters are then used for sampling the respective SVCs.
nugget	(numeric(1)) Variance of the nugget / error term.
seed	(numeric(1)) Seed set within the function for sampling.
given.locs	(NULL or data.frame(n,2)) If NULL, the observations locations are sampled from a regular grid, Otherwise, the data.frame contains the observation locations. The data frame must have two columns of name "x" and "y". The number of observations is then the number of rows n.

**Value**

(data.frame(m\*m, p+3))  
Data frame with p+3 columns: first p are SVCs followed by a nugget and two columns for coordinates, i.e., locations. Number of observations is m\*m.

**Examples**

```
# number of SVC
p <- 3
# sqrt of total number of observations
m <- 20
# covariance parameters
(pars <- data.frame(
  nu = rep(0.5, p),
  var = c(0.1, 0.2, 0.3),
  scale = c(0.3, 0.1, 0.2)
))
nugget.var <- 0.05

# function to sample SVCs
sp.SVC <- fullSVC_reggrid(m = m, p = p,
  cov_pars = pars,
  nugget = nugget.var)

head(sp.SVC)
```

**Description**

Computes the GLS estimate using the formula:

$$\mu_{GLS} = (X^T \Sigma^{-1} X)^{-1} X^T \Sigma^{-1} y.$$

The computation is done depending on the input class of the Cholesky factor R. It relies on the classical `solve` or on using `forwardsolve` and `backsolve` functions of package `spam`, see `solve`. This is much faster than computing the inverse of  $\Sigma$ , especially since we have to compute the Cholesky decomposition of  $\Sigma$  either way.

**Usage**

```
GLS_chol(R, X, y)

## S3 method for class 'spam.chol.NgPeyton'
GLS_chol(R, X, y)

## S3 method for class 'matrix'
GLS_chol(R, X, y)
```

**Arguments**

R	( <code>spam.chol.NgPeyton</code> or <code>matrix(n,n)</code> ) Cholesky factor of the covariance matrix $\Sigma$ . If covariance tapering and sparse matrices are used, then the input is of class <code>spam.chol.NgPeyton</code> . Otherwise, R is the output of a standard <code>chol</code> , i.e., a simple matrix
X	( <code>matrix(n,p)</code> ) Data / design matrix.
y	( <code>numeric(n)</code> ) Response vector

**Value**

A `numeric(p)` vector, i.e., the mean effects.

**Author(s)**

Jakob Dambon

**Examples**

```
# generate data
n <- 10
X <- cbind(1, 20+1:n)
y <- rnorm(n)
A <- matrix(runif(n^2)*2-1, ncol=n)
Sigma <- t(A) %*% A
# two possibilities
## using standard Cholesky decomposition
R_mat <- chol(Sigma); str(R_mat)
```



```

mu_mat <- GLS_chol(R_mat, X, y)
## using spam
R_spam <- chol(as.spam(Sigma)); str(R_spam)
mu_spam <- GLS_chol(R_spam, X, y)
# should be identical to the following
mu <- solve(crossprod(X, solve(Sigma, X))) %%
      crossprod(X, solve(Sigma, y))
## check
abs(mu - mu_mat)
abs(mu - mu_spam)

```

---

house

*Lucas County House Price Data*


---

## Description

A dataset containing the prices and other attributes of 25,357 houses in Lucas County, Ohio. The selling dates span years 1993 to 1998. Data taken from [house](#) (spData package) and slightly modified to a `data.frame`.

## Usage

```
house
```

## Format

A data frame with 25357 rows and 25 variables:

**price** (integer) selling price, in US dollars

**yrbuilt** (integer) year the house was built

**stories** (factor) levels are "one", "bilevel", "multilvl", "one+half", "two", "two+half", "three"

**TLA** (integer) total living area, in square feet.

**wall** (factor) levels are "stucdrvt", "ccbtile", "metlvnyl", "brick", "stone", "wood", "partbrk"

**beds, baths, halfbaths** (integer) number of corresponding rooms / facilities.

**frontage, depth** dimensions of the lot. Unit is feet.

**garage** (factor) levels are "no garage", "basement", "attached", "detached", "carport"

**garagesqft** (integer) garage area, in square feet. If garage == "no garage", then `garagesqft == 0`.

**rooms** (integer) number of rooms

**lotsize** (integer) area of lot, in square feet

**sdate** (Date) selling date, in format yyyy-mm-dd

**avalue** (int) appraised value

**s1993, s1994, s1995, s1996, s1997, s1998** (int) dummies for selling year.

**syear** (factor) levels are selling years "1993", "1994", "1995", "1996", "1997", "1998"

**long, lat** (numeric) location of houses. Longitude and Latitude are given in CRS(+init=epsg:2834), the Ohio North State Plane. Units are meters.

**Source**

<http://www.spatial-econometrics.com/html/jplv6.zip>

---

 IC.SVC\_mle

---

*Conditional Akaike's and Bayesian Information Criteria*


---

**Description**

Methods to calculate information criteria for `SVC_mle` objects. Currently, two are supported: the conditional Akaike's Information Criteria  $cAIC = -2 * \log - likelihood + 2 * (edof + df)$  and the Bayesian Information Criteria  $BIC = -2 * \log - likelihood + \log(n) * npar$ . Note that the Akaike's Information Criteria is of the corrected form, that is:  $edof$  is the effective degrees of freedom which is derived as the trace of the hat matrices and  $df$  is the degree of freedoms with respect to mean parameters.

**Usage**

```
## S3 method for class 'SVC_mle'
BIC(object, ...)

## S3 method for class 'SVC_mle'
AIC(object, conditional = "BW", ...)
```

**Arguments**

<code>object</code>	<code>SVC_mle</code> object
<code>...</code>	further arguments
<code>conditional</code>	string. If <code>conditional = "BW"</code> , the conditional AIC is calculated.

**Value**

numeric, value of information criteria

**Author(s)**

Jakob Dambon

---

init\_bounds\_optim      *Setting of Optimization Bounds and Initial Values*

---

### Description

Sets bounds and initial values for `optim` by extracting potentially given values from `SVC_mle_control` and checking them, or calculating them from given data. See Details.

### Usage

```
init_bounds_optim(control, p, q, id_obj, med_dist, y_var, OLS_mu)
```

### Arguments

control	( <code>SVC_mle_control</code> output, i.e. list)
p	(numeric(1)) Number of fixed effects
q	(numeric(1)) Number of SVCs
id_obj	(numeric(2*q+1+q)) Index vector to identify the arguments of objective function.
med_dist	(numeric(1)) Median distance between observations
y_var	(numeric(1)) Variance of response y
OLS_mu	(numeric(p)) Coefficient estimates of ordinary least squares (OLS).

### Details

If values are not provided, then they are set in the following way. Let  $d$  be the median distance `med_dist`, let  $s_y^2$  be the variance of the response `y_var`, and let  $b_j$  be the OLS coefficients of the linear model. The computed values are given in the table below.

Parameter	Lower bound	Initial Value	Upper Bound
Range	$d/1000$	$d/4$	$10d$
Variance	0	$s_y^2/(q+1)$	$10s_y^2$
Nugget	$10^{-6}$	$s_y^2/(q+1)$	$10s_y^2$
Mean $j$	-Inf	$b_j$	Inf

### Value

A list with three entries: lower, init, and upper.

**Author(s)**

Jakob Dambon

---

logLik.SVC_mle	<i>Extract the Likelihood</i>
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---

**Description**

Method to extract the computed (penalized) log (profile) Likelihood from an [SVC\\_mle](#) object.

**Usage**

```
## S3 method for class 'SVC_mle'  
logLik(object, ...)
```

**Arguments**

object	<a href="#">SVC_mle</a> object
...	further arguments

**Value**

an object of class `logLik` with attributes

- "penalized", logical, if the likelihood (FALSE) or some penalized likelihood (TRUE) was optimized.
- "profileLik", logical, if the optimization was done using the profile likelihood (TRUE) or not.
- "nobs", integer of number of observations
- "df", integer of how many parameters were estimated. **Note:** This includes only the covariance parameters if the profile likelihood was used.

**Author(s)**

Jakob Dambon

---

nlocs	<i>Extract Number of Unique Locations Function to extract the number of unique locations in the data set used in an MLE of the <a href="#">SVC_mle</a> object.</i>
-------	--

---

**Description**

Extract Number of Unique Locations

Function to extract the number of unique locations in the data set used in an MLE of the [SVC\\_mle](#) object.

**Usage**

```
nlocs(object)
```

**Arguments**

object            [SVC\\_mle](#) object

**Value**

integer with the number of unique locations

**Author(s)**

Jakob Dambon

---

nobs.SVC_mle	<i>Extact Number of Observations</i>
--------------	--------------------------------------

---

**Description**

Method to extract the number of observations used in MLE for an [SVC\\_mle](#) object.

**Usage**

```
## S3 method for class 'SVC_mle'
nobs(object, ...)
```

**Arguments**

object            [SVC\\_mle](#) object  
 ...               further arguments

**Value**

an integer of number of observations

**Author(s)**

Jakob Dambon

---

own\_dist                      *Computes (Cross-) Distances*

---

**Description**

Computes (Cross-) Distances

**Usage**

```
own_dist(x, y = NULL, taper = NULL, ...)
```

**Arguments**

x	(matrix) Matrix containing locations
y	(NULL or matrix) If NULL, computes the distances between x. Otherwise, computes cross-distances, i.e., pair-wise distances between rows of x and y.
taper	(NULL or numeric(1)) If NULL, all distances are considered. Otherwise, only distances shorter than taper are used. Hence the output will be a sparse matrix of type <a href="#">spam</a> .
...	Further arguments for either <a href="#">dist</a> or <a href="#">nearest.dist</a> .

**Value**

A matrix or spam object.

---

`plot.SVC_mle`*Plotting Residuals of SVC\_mle model*

---

**Description**

Method to plot the residuals from an `SVC_mle` object. For this, `save.fitted` has to be `TRUE` in `SVC_mle_control`.

**Usage**

```
## S3 method for class 'SVC_mle'  
plot(x, which = 1:2, ...)
```

**Arguments**

<code>x</code>	( <code>SVC_mle</code> )
<code>which</code>	(numeric) A numeric vector and subset of 1:2 indicating which of the 2 plots should be plotted.
<code>...</code>	further arguments

**Value**

a maximum 2 plots

- Tukey-Anscombe plot, i.e. residuals vs. fitted
- QQ-plot

**Author(s)**

Jakob Dambon

**See Also**

[legend SVC\\_mle](#)

**Examples**

```
##' ## ---- toy example ----  
## sample data  
# setting seed for reproducibility  
set.seed(123)  
m <- 7  
# number of observations  
n <- m*m  
# number of SVC  
p <- 3  
# sample data
```

```

y <- rnorm(n)
X <- matrix(rnorm(n*p), ncol = p)
# locations on a regular m-by-m-grid
locs <- expand.grid(seq(0, 1, length.out = m),
                   seq(0, 1, length.out = m))

## preparing for maximum likelihood estimation (MLE)
# controls specific to MLE
control <- SVC_mle_control(
  # initial values of optimization
  init = rep(0.1, 2*p+1),
  # using profile likelihood
  profileLik = TRUE
)

# controls specific to optimization procedure, see help(optim)
opt.control <- list(
  # number of iterations (set to one for demonstration sake)
  maxit = 1,
  # tracing information
  trace = 6
)

## starting MLE
fit <- SVC_mle(y = y, X = X, locs = locs,
              control = control,
              optim.control = opt.control)

## output: convergence code equal to 1, since maxit was only 1
summary(fit)

## plot residuals
# only QQ-plot
plot(fit, which = 2)

# two plots next to each other
oldpar <- par(mfrow = c(1, 2))
plot(fit)
par(oldpar)

```

---

predict.SVC\_mle

*Prediction of SVCs (and response variable)*


---

## Description

Prediction of SVCs (and response variable)



**Usage**

```
## S3 method for class 'SVC_mle'
predict(
  object,
  newlocs = NULL,
  newX = NULL,
  newW = NULL,
  compute.y.var = FALSE,
  ...
)
```

**Arguments**

object	(SVC_mle) Model obtained from <a href="#">SVC_mle</a> function call.
newlocs	(NULL or <code>matrix(n.new,2)</code> ) If NULL, then function uses observed locations of model to estimate SVCs. Otherwise, these are the new locations the SVCs are predicted for.
newX	(NULL or <code>matrix(n.new,q)</code> ) If provided (together with newW), the function also returns the predicted response variable.
newW	(NULL or <code>matrix(n.new,p)</code> ) If provided (together with newX), the function also returns the predicted response variable.
compute.y.var	(logical(1)) If TRUE and the response is being estimated, the predictive variance of each estimate will be computed.
...	further arguments

**Value**

The function returns a data frame of `n.new` rows and with columns

- `SVC_1, ..., SVC_p`: the predicted SVC at locations `newlocs`.
- `y.pred`, if `newX` and `newW` are provided
- `y.var`, if `newX` and `newW` are provided and `compute.y.var` is set to TRUE.
- `loc_x, loc_y`, the locations of the predictions

**Author(s)**

Jakob Dambon

**References**

Dambon, J. A., Sigrist, F., Furrer, R. (2021) *Maximum likelihood estimation of spatially varying coefficient models for large data with an application to real estate price prediction*, Spatial Statistics doi: [10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470)

**See Also**[SVC\\_mle](#)**Examples**

```
## ---- toy example ----
## sample data
# setting seed for reproducibility
set.seed(123)
m <- 7
# number of observations
n <- m*m
# number of SVC
p <- 3
# sample data
y <- rnorm(n)
X <- matrix(rnorm(n*p), ncol = p)
# locations on a regular m-by-m-grid
locs <- expand.grid(seq(0, 1, length.out = m),
                   seq(0, 1, length.out = m))

## preparing for maximum likelihood estimation (MLE)
# controls specific to MLE
control <- SVC_mle_control(
  # initial values of optimization
  init = rep(0.1, 2*p+1),
  # lower bound
  lower = rep(1e-6, 2*p+1),
  # using profile likelihood
  profileLik = TRUE
)

# controls specific to optimization procedure, see help(optim)
opt.control <- list(
  # number of iterations (set to one for demonstration sake)
  maxit = 1,
  # tracing information
  trace = 6
)

## starting MLE
fit <- SVC_mle(y = y, X = X, locs = locs,
              control = control,
              optim.control = opt.control)

## output: convergence code equal to 1, since maxit was only 1
summary(fit)

## prediction
# new location
newlocs <- matrix(0.5, ncol = 2, nrow = 2)
```

```

# new data
X.new <- matrix(rnorm(2*p), ncol = p)

# predicting SVCs
predict(fit, newlocs = newlocs)

# predicting SVCs and calculating response
predict(fit, newlocs = newlocs,
        newX = X.new, newW = X.new)

# predicting SVCs, calculating response and predictive variance
predict(fit, newlocs = newlocs,
        newX = X.new, newW = X.new,
        compute.y.var = TRUE)

```

---

```

prep_par_output      Preparation of Parameter Output

```

---

### Description

Prepares and computes the ML estimates and their respective standard errors.

### Usage

```
prep_par_output(output_par, Sigma_final, Rstruct, profileLik, X, y, H, q)
```

### Arguments

output_par	(numeric) Found optimal value of <code>optim</code> .
Sigma_final	(spam or matrix(n,n)) Covariance matrix Sigma of SVC under final covariance parameters.
Rstruct	(NULL or spam.chol.NgPeyton) If covariance tapering is used, the Cholesky factor has been calculated previously and can be used to efficiently update the Cholesky factor of Sigma_final, which is an spam object.
profileLik	(logical(1)) Indicates if optimization has been conducted over full or profile likelihood.
X	(matrix(n,p)) Design matrix
y	(numeric(p)) Response vector
H	(NULL or matrix) Hessian of MLE
q	(numeric(1)) Number of SVC

### Value

A list with two data.frame. Each contains the estimated parameters with their standard errors of the fixed and random effects, respectively.

---

```
print.summary.SVC_mle Printing Method for summary.SVC_mle
```

---

**Description**

Printing Method for `summary.SVC_mle`

**Usage**

```
## S3 method for class 'summary.SVC_mle'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

**Arguments**

<code>x</code>	<code>summary.SVC_mle</code>
<code>digits</code>	the number of significant digits to use when printing.
<code>...</code>	further arguments

**Value**

The printed output of the summary in the console.

**See Also**

[summary.SVC\\_mle](#) [SVC\\_mle](#)

---

```
print.SVC_mle Print Method for SVC_mle
```

---

**Description**

Method to print an `SVC_mle` object.

**Usage**

```
## S3 method for class 'SVC_mle'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

**Arguments**

<code>x</code>	<code>SVC_mle</code> object
<code>digits</code>	(numeric) Number of digits to be plotted.
<code>...</code>	further arguments

**Author(s)**

Jakob Dambon

---

residuals.SVC_mle	<i>Extract Model Residuals</i>
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---

**Description**

Method to extract the residuals from an `SVC_mle` object. This is only possible if `save.fitted` was set to `TRUE`.

**Usage**

```
## S3 method for class 'SVC_mle'
residuals(object, ...)
```

**Arguments**

<code>object</code>	<code>SVC_mle</code> object
<code>...</code>	further arguments

**Value**

(numeric(n)) Residuals of model

**Author(s)**

Jakob Dambon

---

sample_fullSVC	<i>Sample Function for GP-based SVC Model for Given Locations</i>
----------------	---

---

**Description**

Samples SVC data at given locations. The SVCs parameters and the covariance function have to be provided. The sampled model matrix contains an intercept as a first column and further covariates sampled from a standard normal. The SVCs are sampled according to their given parametrization and at respective observation locations. The error vector sampled from a nugget effect. Finally, the response vector is computed.

**Usage**

```
sample_fullSVC(
  df.pars,
  nugget.sd,
  locs,
  cov.name = c("exp", "sph", "mat32", "mat52", "wend1", "wend2")
)
```

**Arguments**

<code>df.pars</code>	( <code>data.frame(p, 3)</code> ) Contains the mean and covariance parameters of SVCs. The three columns must have the names "mean", "var", and "scale".
<code>nugget.sd</code>	( <code>numeric(1)</code> ) Standard deviation of the nugget / error term.
<code>locs</code>	( <code>numeric(n)</code> or <code>matrix(n,d)</code> ) The numeric vector or matrix contains the observation locations and therefore defines the number of observations to be n. For a vector, we assume locations on the real line, i.e., $d = 1$ .
<code>cov.name</code>	( <code>character(1)</code> ) Character defining the covariance function, c.f. <a href="#">SVC_mle_control</a> .

**Value**

`list`  
Returns a list with the response  $y$ , model matrix  $X$ , a matrix  $\beta$  containing the sampled SVC at given locations, a vector  $\epsilon$  containing the error, and a matrix  $locs$  containing the original locations.

**Examples**

```
set.seed(123)
# SVC parameters
(df.pars <- data.frame(
  var = c(2, 1),
  scale = c(3, 1),
  mean = c(1, 2)))
# nugget standard deviation
tau <- 0.5

# sample locations
s <- sort(runif(500, min = 0, max = 10))
SVCdata <- sample_fullSVC(
  df.pars = df.pars, nugget.sd = tau, locs = s, cov.name = "mat32"
)
```

**Description**

Builds the covariance matrix of  $y$  (p. 6, Dambon et al. (2021) doi: [10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470)) for a given set of covariance parameters and other, pre-defined objects (like the outer-products, covariance function, and, possibly, a taper matrix).

**Usage**

```
Sigma_y(x, cov_func, outer.W, taper = NULL)
```

**Arguments**

x	(numeric(2q+1)) Non negative vector containing the covariance parameters in the following order: $\rho_1, \sigma_1^2, \dots, \rho_q, \sigma_q^2, \tau^2$ . Note that the odd entries, i.e., the ranges and the nugget variance, have to be greater than 0, otherwise the covariance matrix is not well-defined (singularities or not-invertible).
cov_func	(function) A covariance function that works on the pre-defined distance matrix d. It takes a numeric vector as an input, the first entry being the range, the second being the variance (also called partial sill). Usually, it is defined as, e.g.: <code>function(pars) spam: : cov.exp(d, pars)</code> or any other covariance function defined for two parameters.
outer.W	(list(q)) A list of length q containing the outer products of the random effect covariates in a lower triangular, (possibly sparse) matrix. If tapering is applied, the list entries, i.e., the outer products have to be given as <code>spam</code> objects.
taper	(NULL or spam) If covariance tapering is applied, this argument contains the taper matrix, which is a <code>spam</code> object. Otherwise, it is NULL.

**Value**

Returns a positive-definite covariance matrix y, which is needed in the MLE. Specifically, a Cholesky Decomposition is applied on the covariance matrix.

**Author(s)**

Jakob Dambon

**References**

Dambon, J. A., Sigrist, F., Furrer, R. (2021) *Maximum likelihood estimation of spatially varying coefficient models for large data with an application to real estate price prediction*, Spatial Statistics doi: [10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470)

**Examples**

```
# locations
locs <- 1:6
# random effects covariates
W <- cbind(rep(1, 6), 5:10)
# distance matrix with and without tapering
d <- as.matrix(dist(locs))
# distance matrix with and without tapering
tap_dist <- 2
```

```

d_tap <- spam::nearest.dist(locs, delta = tap_dist)
# call without tapering
(Sy <- varycoef:::Sigma_y(
  x = rep(0.5, 5),
  cov_func = function(x) spam::cov.exp(d, x),
  outer.W = lapply(1:ncol(W), function(k) W[, k] %o% W[, k])
))
str(Sy)
# call with tapering
(Sy_tap <- varycoef:::Sigma_y(
  x = rep(0.5, 5),
  cov_func = function(x) spam::cov.exp(d_tap, x),
  outer.W = lapply(1:ncol(W), function(k)
    spam::as.spam((W[, k] %o% W[, k]) * (d_tap<=tap_dist))
  ),
  taper = spam::cov.wend1(d_tap, c(tap_dist, 1, 0))
))
str(Sy_tap)
# difference between tapered and untapered covariance matrices
Sy-Sy_tap

```

---

summary.SVC\_mle

*Summary Method for SVC\_mle*


---

## Description

Method to construct a `summary.SVC_mle` object out of a `SVC_mle` object.

## Usage

```
## S3 method for class 'SVC_mle'
summary(object, ...)
```

## Arguments

<code>object</code>	<code>SVC_mle</code> object
<code>...</code>	further arguments

## Value

object of class `summary.SVC_mle` with summarized values of the MLE.

## Author(s)

Jakob Dambon

## See Also

[SVC\\_mle](#)



---

`SVC_mle`*MLE of SVC model*

---

### Description

Conducts a maximum likelihood estimation (MLE) for a Gaussian process-based SVC model as described in Dambon et al. (2021) doi: [10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470). More specifically, the model is defined as:

$$y(s) = X\mu + W\eta(s) + \epsilon(s)$$

where:

- $y$  is the response (vector of length  $n$ )
- $X$  is the data matrix for the fixed effects covariates. The dimensions are  $n$  times  $p$ . This leads to  $p$  fixed effects.
- $\mu$  is the vector containing the fixed effects
- $W$  is the data matrix for the SVCs modeled by GPs. The dimensions are  $n$  times  $q$ . This leads to  $q$  SVCs in the model.
- $\eta$  are the SVCs represented by a GP.
- $\epsilon$  is the nugget effect

The MLE is a numeric optimization that runs `optim` or (if parallelized) `optimParallel`.

### Usage

```
SVC_mle(...)  
  
## Default S3 method:  
SVC_mle(y, X, locs, W = NULL, control = NULL, optim.control = list(), ...)  
  
## S3 method for class 'formula'  
SVC_mle(  
  formula,  
  data,  
  RE_formula = NULL,  
  locs,  
  control,  
  optim.control = list(),  
  ...  
)
```

**Arguments**

...	further arguments
y	(numeric(n)) Response vector.
X	(matrix(n,p)) Design matrix. Intercept has to be added manually.
locs	(matrix(n,d)) Locations in a $d$ -dimensional space. May contain multiple observations at single location.
W	(NULL or matrix(n,q)) If NULL, the same matrix as provided in X is used. This fits a full SVC model, i.e., each covariate effect is modeled with a mean and an SVC. In this case we have $p = q$ . If optional matrix W is provided, SVCs are only modeled for covariates within matrix W.
control	(list) Control paramaters given by <a href="#">SVC_mle_control</a> .
optim.control	(list) Control arguments for optimization function, see Details in <a href="#">optim</a> .
formula	Formula describing the fixed effects in SVC model. The response, i.e. LHS of the formula, is not allowed to have functions such as <code>sqrt()</code> or <code>log()</code> .
data	data frame containing the observations
RE_formula	Formula describing the random effects in SVC model. Only RHS is considered. If NULL, the same RHS of argument formula for fixed effects is used.

**Value**

Object of class `SVC_mle` if `control$extract_fun = FALSE`, meaning that a MLE has been conducted. Otherwise, if `control$extract_fun = TRUE`, the function returns a list with two entries:

- `obj_fun`: the objective function used in the optimization
- `args`: the arguments to evaluate the objective function.

For further detials, see description of [SVC\\_mle\\_control](#).

**Author(s)**

Jakob Dambon

**References**

Dambon, J. A., Sigrist, F., Furrer, R. (2021) *Maximum likelihood estimation of spatially varying coefficient models for large data with an application to real estate price prediction*, Spatial Statistics doi: [10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470)

**See Also**

[predict.SVC\\_mle](#)

**Examples**

```

## ---- toy example ----
## sample data
# setting seed for reproducibility
set.seed(123)
m <- 7
# number of observations
n <- m*m
# number of SVC
p <- 3
# sample data
y <- rnorm(n)
X <- matrix(rnorm(n*p), ncol = p)
# locations on a regular m-by-m-grid
locs <- expand.grid(seq(0, 1, length.out = m),
                    seq(0, 1, length.out = m))

## preparing for maximum likelihood estimation (MLE)
# controls specific to MLE
control <- SVC_mle_control(
  # initial values of optimization
  init = rep(0.1, 2*p+1),
  # lower bound
  lower = rep(1e-6, 2*p+1),
  # using profile likelihood
  profileLik = TRUE
)

# controls specific to optimization procedure, see help(optim)
opt.control <- list(
  # number of iterations (set to one for demonstration sake)
  maxit = 1,
  # tracing information
  trace = 6
)

## starting MLE
fit <- SVC_mle(y = y, X = X, locs = locs,
              control = control,
              optim.control = opt.control)
class(fit)

## output: convergence code equal to 1, since maxit was only 1
summary(fit)

## extract the optimization arguments, including objective function
control$extract_fun <- TRUE
opt <- SVC_mle(y = y, X = X, locs = locs,
              control = control)

# objective function and its arguments of optimization
class(opt$obj_fun)

```

```

class(opt$args)

# single evaluation with initial value
do.call(opt$obj_fun,
        c(list(x = control$init), opt$args))

## ---- real data example ----
require(sp)
## get data set
data("meuse", package = "sp")

# construct data matrix and response, scale locations
y <- log(meuse$cadmium)
X <- model.matrix(~1+dist+lime+elev, data = meuse)
locs <- as.matrix(meuse[, 1:2])/1000

## starting MLE
# the next call takes a couple of seconds
fit <- SVC_mle(y = y, X = X, locs = locs,
              # has 4 fixed effects, but only 3 random effects (SVC)
              # elev is missing in SVC
              W = X[, 1:3],
              control = SVC_mle_control(
                # initial values for 3 SVC
                # 7 = (3 * 2 covariance parameters + nugget)
                init = c(rep(c(0.4, 0.2), 3), 0.2),
                profileLik = TRUE
              ))

## summary and residual output
summary(fit)
plot(fit)

## predict
# new locations
newlocs <- expand.grid(
  x = seq(min(locs[, 1]), max(locs[, 1]), length.out = 30),
  y = seq(min(locs[, 2]), max(locs[, 2]), length.out = 30))
# predict SVC for new locations
SVC <- predict(fit, newlocs = as.matrix(newlocs))
# visualization
sp.SVC <- SVC
coordinates(sp.SVC) <- ~loc_1+loc_2
spplot(sp.SVC, colorkey = TRUE)

```

**Description**

Function to set up control parameters for `SVC_mle`. In the following, we assume the GP-based SVC model to have  $q$  GPs which model the SVCs and  $p$  fixed effects.

**Usage**

```
SVC_mle_control(...)

## Default S3 method:
SVC_mle_control(
  cov.name = c("exp", "sph", "mat32", "mat52", "wend1", "wend2"),
  tapering = NULL,
  parallel = NULL,
  init = NULL,
  lower = NULL,
  upper = NULL,
  save.fitted = TRUE,
  profileLik = FALSE,
  mean.est = c("GLS", "OLS"),
  pc.prior = NULL,
  extract_fun = FALSE,
  hessian = TRUE,
  dist = list(method = "euclidean"),
  ...
)

## S3 method for class 'SVC_mle'
SVC_mle_control(object, ...)
```

**Arguments**

<code>...</code>	Further Arguments yet to be implemented
<code>cov.name</code>	(character(1)) Name of the covariance function of the GPs. Currently, the following are implemented: "exp" for the exponential, "sph" for spherical, "mat32" and "mat52" for Matern class covariance functions with smoothness 3/2 or 5/2, as well as "wend1" and "wend2" for Wendland class covariance functions with kappa 1 or 2.
<code>tapering</code>	(NULL or numeric(1)) If NULL, no tapering is applied. If a scalar is given, covariance tapering with this taper range is applied, for all Gaussian processes modeling the SVC. Only defined for Matern class covariance functions, i.e., set <code>cov.name</code> either to "exp", "mat32", or "mat52".
<code>parallel</code>	(NULL or list) If NULL, no parallelization is applied. If cluster has been established, define arguments for parallelization with a list, see documentation of <code>optimParallel</code> . See Examples.

init	(NULL or numeric(2q+1+p*as.numeric(profileLik))) Initial values for optimization procedure. If NULL is given, an initial vector is calculated (see Details). Otherwise, the vector is assumed to consist of q-times (alternating) range and variance, the nugget variance and if profileLik = TRUE p mean effects.
lower	(NULL or numeric(2q+1+p*as.numeric(profileLik))) Lower bound for init in optim. Default NULL calculates the lower bounds (see Details).
upper	(NULL or numeric(2q+1+p*as.numeric(profileLik))) Upper bound for init in optim. Default NULL calculates the upper bounds (see Details).
save.fitted	(logical(1)) If TRUE, calculates the fitted values and residuals after MLE and stores them. This is necessary to call <code>residuals</code> and <code>fitted</code> methods afterwards.
profileLik	(logical(1)) If TRUE, MLE is done over profile Likelihood of covariance parameters.
mean.est	(character(1)) If profileLik = TRUE, the means have to be estimated separately for each step. "GLS" uses the generalized least square estimate while "OLS" uses the ordinary least squares estimate.
pc.prior	(NULL or numeric(4)) If numeric vector is given, penalized complexity priors are applied. The order is $\rho_0, \alpha_\rho, \sigma_0, \alpha_\sigma$ to give some prior beliefs for the range and the standard deviation of GPs, such that $P(\rho < \rho_0) = \alpha_\rho, P(\sigma > \sigma_0) = \alpha_\sigma$ . This regulates the optimization process. Currently, only supported for GPs with of Matérn class covariance functions. Based on the idea by Fulgstad et al. (2018) doi: <a href="https://doi.org/10.1080/01621459.2017.1415907">10.1080/01621459.2017.1415907</a> .
extract_fun	(logical(1)) If TRUE, the function call of <code>SVC_mle</code> stops before the MLE and gives back the objective function of the MLE as well as all used arguments. If FALSE, regular MLE is conducted.
hessian	(logical(1)) If TRUE, Hessian matrix is computed, see <code>optim</code> . This required to give the standard errors for covariance parameters and to do a Wald test on the variances, see <code>summary.SVC_mle</code> .
dist	(list) List containing the arguments of <code>dist</code> or <code>nearest.dist</code> . This controls the method of how the distances and therefore dependency structures are calculated. The default gives Euclidean distances in a $d$ -dimensional space. Further editable arguments are <code>p, miles, R</code> , see respective help files of <code>dist</code> or <code>nearest.dist</code> .
object	(SVC_mle) The function then extracts the control settings from the function call used to compute in the given <code>SVC_mle</code> object.

## Details

If not provided, the initial values as well as the lower and upper bounds are calculated given the provided data. In particular, we require the median distance between observations, the variance of the response and, the ordinary least square (OLS) estimates, see [init\\_bounds\\_optim](#).

The argument `extract_fun` is useful, when one wants to modify the objective function. Further, when trying to parallelize the optimization, it is useful to check whether a single evaluation of the objective function takes longer than 0.05 seconds to evaluate, cf. Gerber and Furrer (2019) doi: [10.32614/RJ2019030](https://doi.org/10.32614/RJ2019030). Platform specific issues can be sorted out by the user by setting up their own optimization.

## Value

A list with which `SVC_mle` can be controlled.

## Author(s)

Jakob Dambon

## See Also

[SVC\\_mle](#)

## Examples

```
control <- SVC_mle_control(init = rep(0.3, 10))
# or
control <- SVC_mle_control()
control$init <- rep(0.3, 10)

# Code for setting up parallel computing
require(parallel)
# exchange number of nodes (1) for detectCores()-1 or appropriate number
cl <- makeCluster(1, setup_strategy = "sequential")
clusterEvalQ(
  cl = cl,
  {
    library(spam)
    library(varycoef)
  })
# use this list for parallel argument in SVC_mle_control
parallel.control <- list(cl = cl, forward = TRUE, loginfo = TRUE)
# SVC_mle goes here ...
# DO NOT FORGET TO STOP THE CLUSTER!
stopCluster(cl); rm(cl)
```

---

`SVC_selection`*SVC Model Selection*

---

**Description**

This function implements the variable selection for Gaussian process-based SVC models using a penalized maximum likelihood estimation (PMLE, Dambon et al., 2021, <arXiv:2101.01932>). It jointly selects the fixed and random effects of GP-based SVC models.

**Usage**

```
SVC_selection(obj.fun, mle.par, control, ...)
```

**Arguments**

<code>obj.fun</code>	( <code>SVC_obj_fun</code> ) Function of class <code>SVC_obj_fun</code> . This is the output of <code>SVC_mle</code> with the <code>SVC_mle_control</code> parameter <code>extract_fun</code> set to <code>TRUE</code> . This objective function comprises of the whole SVC model on which the selection should be applied.
<code>mle.par</code>	( <code>numeric(2*q+1)</code> ) Numeric vector with estimated covariance parameters of unpenalized MLE.
<code>control</code>	( <code>list</code> ) List of control parameters for variable selection. Output of <code>SVC_selection_control</code> .
<code>...</code>	Further arguments.

**Value**

Returns an object of class `SVC_selection`. It contains parameter estimates under PMLE and the optimization as well as choice of the shrinkage parameters.

**Author(s)**

Jakob Dambon

**References**

Dambon, J. A., Sigrist, F., Furrer, R. (2021). *Joint Variable Selection of both Fixed and Random Effects for Gaussian Process-based Spatially Varying Coefficient Models*, ArXiv Preprint <https://arxiv.org/abs/2101.01932>



---

SVC\_selection\_control *SVC Selection Parameters*


---

**Description**

Function to set up control parameters for `SVC_selection`. The underlying Gaussian Process-based SVC model is defined in `SVC_mle`. `SVC_selection` then jointly selects fixed and random effects of the GP-based SVC model using a penalized maximum likelihood estimation (PMLE). In this function, one can set the parameters for the PMLE and its optimization procedures (Dambon et al., 2021, <arXiv:2101.01932>).

**Usage**

```
SVC_selection_control(
  IC.type = c("BIC", "cAIC_BW", "cAIC_VB"),
  method = c("grid", "MBO"),
  r.lambda = c(1e-10, 10),
  n.lambda = 10L,
  n.init = 10L,
  n.iter = 10L,
  CD.conv = list(N = 20L, delta = 1e-06, logLik = TRUE),
  hessian = FALSE,
  adaptive = FALSE,
  parallel = NULL,
  optim.args = list()
)
```

**Arguments**

IC.type	(character(1)) Select Information Criterion.
method	(character(1)) Select optimization method for lambdas, i.e., shrinkage parameters. Either model-based optimization (MBO, Bischl et al., 2017 <arXiv:1703.03373>) or over grid.
r.lambda	(numeric(2)) Range of lambdas, i.e., shrinkage parameters.
n.lambda	(numeric(1)) If grid method is selected, number of lambdas per side of grid.
n.init	(numeric(1)) If MBO method is selected, number of initial values for surrogate model.
n.iter	(numeric(1)) If MBO method is selected, number of iteration steps of surrogate models.
CD.conv	(list(3)) List containing the convergence conditions, i.e., first entry is the maximum number of iterations, second value is the relative change necessary to stop iteration,

	third is logical to toggle if relative change in log likelihood (TRUE) or rather the parameters themselves (FALSE) is the criteria for convergence.
hessian	(logical(1)) If TRUE, Hessian will be computed for final model.
adaptive	(logical(1)) If TRUE, adaptive LASSO is executed, i.e., the shrinkage parameter is defined as $\lambda_j := \lambda/ \theta_j $ .
parallel	(list) List with arguments for parallelization, see documentation of <code>optimParallel</code> .
optim.args	(list) List of further arguments of <code>optimParallel</code> , such as the lower bounds.

**Value**

A list of control parameters for SVC selection.

**Author(s)**

Jakob Dambon

**References**

Bischl, B., Richter, J., Bossek, J., Horn, D., Thomas, J., Lang, M. (2017). *mlrMBO: A Modular Framework for Model-Based Optimization of Expensive Black-Box Functions*, ArXiv preprint <https://arxiv.org/abs/1703.03373>

Dambon, J. A., Sigrist, F., Furrer, R. (2021). *Joint Variable Selection of both Fixed and Random Effects for Gaussian Process-based Spatially Varying Coefficient Models*, ArXiv preprint <https://arxiv.org/abs/2101.01932>

**Examples**

```
# Initializing parameters and switching logLik to FALSE
selection_control <- SVC_selection_control(
  CD.conv = list(N = 20L, delta = 1e-06, logLik = FALSE)
)
# or
selection_control <- SVC_selection_control()
selection_control$CD.conv$logLik <- FALSE
```

## Description

This package offers functions to estimate and predict Gaussian process-based spatially varying coefficient (SVC) models. Briefly described, one generalizes a linear regression equation such that the coefficients are no longer constant, but have the possibility to vary spatially. This is enabled by modeling the coefficients using Gaussian processes with (currently) either an exponential or spherical covariance function. The advantages of such SVC models are that they are usually quite easy to interpret, yet they offer a very high level of flexibility.

## Estimation and Prediction

The ensemble of the function `SVC_mle` and the method `predict` estimates the defined SVC model and gives predictions of the SVC as well as the response for some pre-defined locations. This concept should be rather familiar as it is the same for the classical regression (`lm`) or local polynomial regression (`loess`), to name a couple. As the name suggests, we are using a *maximum likelihood estimation* (MLE) approach in order to estimate the model. The predictor is obtained by the empirical best linear unbiased predictor. to give location-specific predictions. A detailed tutorial with examples is given in a vignette; call `vignette("example", package = "varycoef")`. We also refer to the original article Dambon et al. (2021a) which lays the methodological foundation of this package.

With the before mentioned `SVC_mle` function one gets an object of class `SVC_mle`. And like the method `predict` for predictions, there are several more methods in order to diagnose the model, see `methods(class = "SVC_mle")`.

## Variable Selection

As of version 0.3.0 of `varycoef`, a joint variable selection of both fixed and random effect of the Gaussian process-based SVC model is implemented. It uses a *penalized maximum likelihood estimation* (PMLE) which is implemented via a gradient descent. The estimation of the shrinkage parameter is available using a *model-based optimization* (MBO). Here, we use the framework by Bischl et al. (2017). The methodological foundation of the PMLE is described in Dambon et al. (2021b).

## Author(s)

Jakob Dambon

## References

Bischl, B., Richter, J., Bossek, J., Horn, D., Thomas, J., Lang, M. (2017). *mlrMBO: A Modular Framework for Model-Based Optimization of Expensive Black-Box Functions*, ArXiv preprint <https://arxiv.org/abs/1703.03373>

Dambon, J. A., Sigrist, F., Furrer, R. (2021a) *Maximum likelihood estimation of spatially varying coefficient models for large data with an application to real estate price prediction*, Spatial Statistics 41 100470 doi: [10.1016/j.spasta.2020.100470](https://doi.org/10.1016/j.spasta.2020.100470)

Dambon, J. A., Sigrist, F., Furrer, R. (2021b). *Joint Variable Selection of both Fixed and Random Effects for Gaussian Process-based Spatially Varying Coefficient Models*, ArXiv Preprint <https://arxiv.org/abs/2101.01932>

### Examples

```
vignette("manual", package = "varycoef")  
methods(class = "SVC_mle")
```

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