

# Package ‘gMOIP’

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**Type** Package

**Title** '2D and 3D plots of linear mathematical programming models'

**Version** 1.3.0

**URL** <https://github.com/relund/gMOIP/>

**BugReports** <https://github.com/relund/gMOIP/issues>

**Description** Make 2D and 3D plots of the polytope of a LP, ILP or MILP problem, including integer points and iso profit curve. Can also make a plot of the bi-objective criterion space.

**License** GPL (>= 3.3.2)

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 6.1.1

**Depends** R (>= 3.5.0)

**Imports** ggrepel, geometry, ggplot2, rgl, MASS, plyr

**Suggests** tikzDevice, grid, gridExtra, knitr, rmarkdown

**VignetteBuilder** knitr

**NeedsCompilation** no

**Author** Lars Relund [aut, cre]

**Maintainer** Lars Relund <lars@relund.dk>

**Repository** CRAN

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## R topics documented:

cornerPoints . . . . .	2
cornerPointsCont . . . . .	3
criterionPoints . . . . .	3
df2String . . . . .	4
gMOIP . . . . .	5

hullSegment . . . . .	5
inHull . . . . .	6
integerPoints . . . . .	7
loadView . . . . .	8
mergeLists . . . . .	9
plotCriterion2D . . . . .	9
plotPolytope . . . . .	14
plotPolytope2D . . . . .	21
plotPolytope3D . . . . .	22
saveView . . . . .	23
slices . . . . .	24

<b>Index</b>	<b>26</b>
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cornerPoints	<i>Calculate the corner points for the polytope <math>Ax \leq 0</math>.</i>
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### Description

Calculate the corner points for the polytope  $Ax \leq 0$ .

### Usage

```
cornerPoints(A, b, type = rep("c", ncol(A)), nonneg = rep(TRUE,
  ncol(A)))
```

### Arguments

A	Constraint matrix.
b	Right hand side.
type	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.

### Value

A data frame with a corner point in each row.

### Author(s)

Lars Relund <lars@relund.dk>

**Examples**

```
A <- matrix( c(3,-2, 1, 2, 4,-2,-3, 2, 1), nc = 3, byrow = TRUE)
b <- c(10, 12, 3)
cornerPoints(A, b, type = c("c", "c", "c"))
cornerPoints(A, b, type = c("i", "i", "i"))
cornerPoints(A, b, type = c("i", "c", "c"))
```

---

cornerPointsCont	<i>Calculate the corner points for the polytope <math>Ax \leq b</math> assuming all variables are continuous.</i>
------------------	---

---

**Description**

Calculate the corner points for the polytope  $Ax \leq b$  assuming all variables are continuous.

**Usage**

```
cornerPointsCont(A, b, nonneg = rep(TRUE, ncol(A)))
```

**Arguments**

A	Constraint matrix.
b	Right hand side.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.

**Value**

A data frame with a corner point in each row.

**Author(s)**

Lars Relund <lars@relund.dk>

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critierionPoints	<i>Calculate the criterion points of a set of points and ranges to find the set of non-dominated points (Pareto points) and classify them into extreme supported, non-extreme supported, non-supported.</i>
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**Description**

Calculate the criterion points of a set of points and ranges to find the set of non-dominated points (Pareto points) and classify them into extreme supported, non-extreme supported, non-supported.

**Usage**

```
criterionPoints(points, obj, crit, labels = "coord")
```

**Arguments**

points	A data frame with a column for each variable in the solution space (can also be a rangePoints).
obj	A p x n matrix(one row for each criterion).
crit	Either max or min.
labels	If NULL or "n" don't add any labels (empty string). If 'coord' labels are the solution space coordinates. Otherwise number all points from one based on the solution space points.

**Value**

A data frame with columns x1, ..., xn, z1, ..., zp, lbl (label), nD (non-dominated), ext (extreme), nonExt (non-extreme supported).

**Author(s)**

Lars Relund <lars@relund.dk>

**Examples**

```
A <- matrix( c(3, -2, 1, 2, 4, -2, -3, 2, 1), nc = 3, byrow = TRUE)
b <- c(10,12,3)
points <- integerPoints(A, b)
obj <- matrix( c(1,-3,1,-1,1,-1), byrow = TRUE, ncol = 3 )
criterionPoints(points, obj, crit = "max", labels = "numb")
```

---

df2String

---

*Convert each row to a string.*


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**Description**

Convert each row to a string.

**Usage**

```
df2String(df, round = 2)
```

**Arguments**

df	Data frame.
round	How many digits to round

**Value**

A vector of strings.

gMOIP

*2D plots of linear/integer programming models.***Description**

Make 2D and 3D plots of the polytope of a linear programming (LP), integer linear programming (ILP) model, or mixed integer linear programming (MILP) model with 2 or 3 variables, including integer points, ranges and iso profit curve.

**Details**

Can also make a plot of the bi-objective criterion space and the non-dominated (Pareto) set for bi-objective LP/ILP/MILP programming models.

**Author(s)**

Lars Relund <lars@relund.dk> [aut, cre].

**See Also**

[plotPolytope](#) and [plotCriterion2D](#).

hullSegment

*Find segments (lines) of a face.***Description**

Find segments (lines) of a face.

**Usage**

```
hullSegment(vertices, hull = geometry::convhulln(vertices),
  tol = mean(mean(abs(vertices))) * sqrt(.Machine$double.eps))
```

**Arguments**

vertices	A mxp array of vertices of the convex hull, as used by convhulln.
hull	Tessellation (or triangulation) generated by convhulln. If hull is left empty or not supplied, then it will be generated.
tol	Tolerance on the tests for inclusion in the convex hull. You can think of tol as the distance a point may possibly lie outside the hull, and still be perceived as on the surface of the hull. Because of numerical slop nothing can ever be done exactly here. I might guess a semi-intelligent value of tol to be $\text{tol} = 1.e-13 * \text{mean}(\text{abs}(\text{vertices}(:)))$ . In higher dimensions, the numerical issues of floating point arithmetic will probably suggest a larger value of tol.

**Value**

A matrix with segments.

**Author(s)**

Lars Relund <lars@relund.dk>

---

inHull	<i>Efficient test for points inside a convex hull in n dimensions. Inspired by the Matlab code by John D'Errico <a href="http://www.mathworks.com/matlabcentral/fileexchange/10226-inhull">http://www.mathworks.com/matlabcentral/fileexchange/10226-inhull</a> and <a href="https://tolstoy.newcastle.edu.au/R/e8/help/09/12/8784.html">https://tolstoy.newcastle.edu.au/R/e8/help/09/12/8784.html</a></i>
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**Description**

Efficient test for points inside a convex hull in n dimensions. Inspired by the Matlab code by John D'Errico <http://www.mathworks.com/matlabcentral/fileexchange/10226-inhull> and <https://tolstoy.newcastle.edu.au/R/e8/help/09/12/8784.html>

**Usage**

```
inHull(testPts, vertices, hull = geometry::convhulln(vertices),
      tol = mean(mean(abs(vertices))) * sqrt(.Machine$double.eps))
```

**Arguments**

testPts	A nxp array to test, n data points, in p dimensions If you have many points to test, it is most efficient to call this function once with the entire set.
vertices	A mxp array of vertices of the convex hull, as used by convhulln.
hull	Tessellation (or triangulation) generated by convhulln If hull is left empty or not supplied, then it will be generated.
tol	Tolerance on the tests for inclusion in the convex hull. You can think of tol as the distance a point may possibly lie outside the hull, and still be perceived as on the surface of the hull. Because of numerical slop nothing can ever be done exactly here. I might guess a semi-intelligent value of tol to be $tol = 1.e-13 * mean(abs(vertices(:)))$ In higher dimensions, the numerical issues of floating point arithmetic will probably suggest a larger value of tol.

**Value**

An integer vector of length n

**Author(s)**

Lars Relund <lars@relund.dk>

---

integerPoints      *Integer points in the feasible region ( $Ax \leq b$ ).*

---

**Description**

Integer points in the feasible region ( $Ax \leq b$ ).

**Usage**

```
integerPoints(A, b, nonneg = rep(TRUE, ncol(A)))
```

**Arguments**

A	Constraint matrix.
b	Right hand side.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.

**Value**

A data frame with all integer points inside the feasible region.

**Note**

Do a simple enumeration of all integer points between min and max values found using the continuous polytope.

**Author(s)**

Lars Relund <lars@relund.dk>.

**Examples**

```
A <- matrix( c(3,-2, 1, 2, 4,-2,-3, 2, 1), nc = 3, byrow = TRUE)
b <- c(10, 12, 3)
integerPoints(A, b)
```

```
A <- matrix(c(9, 10, 2, 4, -3, 2), ncol = 2, byrow = TRUE)
b <- c(90, 27, 3)
integerPoints(A, b)
```

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loadView	<i>Help function to load the view angle for the RGL 3D plot from a file or matrix</i>
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---

### Description

Help function to load the view angle for the RGL 3D plot from a file or matrix

### Usage

```
loadView(fname = "view.RData", v = NULL, clear = TRUE,  
         close = FALSE, zoom = 1, ...)
```

### Arguments

fname	The file name of the view.
v	The view matrix.
clear	Call <a href="#">clear3d</a> .
close	Call <a href="#">rgl.close</a> .
zoom	Zoom level.
...	Additional parameters passed to <a href="#">view3d</a> .

### Author(s)

Lars Relund <lars@relund.dk>

### Examples

```
view <- matrix( c(-0.412063330411911, -0.228006735444069, 0.882166087627411, 0,  
0.910147845745087, -0.0574885793030262, 0.410274744033813, 0, -0.042830865830183,  
0.97196090221405, 0.231208890676498, 0, 0, 0, 0, 1), nc = 4)  
  
loadView(v = view)  
A <- matrix( c(3, 2, 5, 2, 1, 1, 1, 1, 3, 5, 2, 4), nc = 3, byrow = TRUE)  
b <- c(55, 26, 30, 57)  
obj <- c(20, 10, 15)  
plotPolytope(A, b, plotOptimum = TRUE, obj = obj, labels = "coord")  
  
# Try to modify the angle in the RGL window  
saveView(print = TRUE) # get the viewangle to insert into R code
```



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mergeLists	<i>Merge two lists to one</i>
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**Description**

Merge two lists to one

**Usage**

```
mergeLists(a, b)
```

**Arguments**

a	First list.
b	Second list.

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plotCriterion2D	<i>Create a plot of the criterion space of a bi-objective problem</i>
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---

**Description**

Create a plot of the criterion space of a bi-objective problem

**Usage**

```
plotCriterion2D(A, b, obj, type = rep("c", ncol(A)), nonneg = rep(TRUE,
  ncol(A)), crit = "max", addTriangles = FALSE, addHull = TRUE,
  plotFeasible = TRUE, latex = FALSE, labels = NULL)
```

**Arguments**

A	The constraint matrix.
b	Right hand side.
obj	A p x n matrix(one row for each criterion).
type	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.
crit	Either max or min (only used if add the iso profit line).
addTriangles	Add search triangles defined by the non-dominated extreme points.
addHull	Add the convex hull and the rays.
plotFeasible	If True then plot the criterion points/slices.
latex	If true make latex math labels for TikZ.
labels	If NULL don't add any labels. If 'n' no labels but show the points. If 'coord' add coordinates to the points. Otherwise number all points from one.

**Value**

The ggplot2 object.

**Note**

Currently only points are checked for dominance. That is, for MILP models some nondominated points may in fact be dominated by a segment.

**Author(s)**

Lars Relund <lars@relund.dk>

**Examples**

```
### Set up 2D plot
# Function for plotting the solution and criterion space in one plot (two variables)
plotBiObj2D <- function(A, b, obj,
  type = rep("c", ncol(A)),
  crit = "max",
  faces = rep("c", ncol(A)),
  plotFaces = TRUE,
  plotFeasible = TRUE,
  plotOptimum = FALSE,
  labels = "numb",
  addTriangles = TRUE,
  addHull = TRUE)
{
  p1 <- plotPolytope(A, b, type = type, crit = crit, faces = faces, plotFaces = plotFaces,
    plotFeasible = plotFeasible, plotOptimum = plotOptimum, labels = labels)
  p2 <- plotCriterion2D(A, b, obj, type = type, crit = crit, addTriangles = addTriangles,
    addHull = addHull, plotFeasible = plotFeasible, labels = labels)
  gridExtra::grid.arrange(p1, p2, nrow = 1)
}

### Bi-objective problem with two variables
A <- matrix(c(-3,2,2,4,9,10), ncol = 2, byrow = TRUE)
b <- c(3,27,90)

## LP model
obj <- matrix(
  c(7, -10, # first criterion
    -10, -10), # second criterion
  nrow = 2)
plotBiObj2D(A, b, obj, addTriangles = FALSE)

## ILP models with different criteria (maximize)
obj <- matrix(c(7, -10, -10, -10), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)))
obj <- matrix(c(3, -1, -2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)))
obj <- matrix(c(-7, -1, -5, 5), nrow = 2)
```

```

plotBiObj2D(A, b, obj, type = rep("i", ncol(A)))
obj <- matrix(c(-1, -1, 2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)))

## ILP models with different criteria (minimize)
obj <- matrix(c(7, -10, -10, -10), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)), crit = "min")
obj <- matrix(c(3, -1, -2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)), crit = "min")
obj <- matrix(c(-7, -1, -5, 5), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)), crit = "min")
obj <- matrix(c(-1, -1, 2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = rep("i", ncol(A)), crit = "min")

# More examples

## MILP model (x1 integer) with different criteria (maximize)
obj <- matrix(c(7, -10, -10, -10), nrow = 2)
plotBiObj2D(A, b, obj, type = c("i", "c"))
obj <- matrix(c(3, -1, -2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = c("i", "c"))
obj <- matrix(c(-7, -1, -5, 5), nrow = 2)
plotBiObj2D(A, b, obj, type = c("i", "c"))
obj <- matrix(c(-1, -1, 2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = c("i", "c"))

## MILP model (x2 integer) with different criteria (minimize)
obj <- matrix(c(7, -10, -10, -10), nrow = 2)
plotBiObj2D(A, b, obj, type = c("c", "i"), crit = "min")
obj <- matrix(c(3, -1, -2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = c("c", "i"), crit = "min")
obj <- matrix(c(-7, -1, -5, 5), nrow = 2)
plotBiObj2D(A, b, obj, type = c("c", "i"), crit = "min")
obj <- matrix(c(-1, -1, 2, 2), nrow = 2)
plotBiObj2D(A, b, obj, type = c("c", "i"), crit = "min")

### Set up 3D plot
# Function for plotting the solution and criterion space in one plot (three variables)
plotBiObj3D <- function(A, b, obj,
                        type = rep("c", ncol(A)),
                        crit = "max",
                        faces = rep("c", ncol(A)),
                        plotFaces = TRUE,
                        plotFeasible = TRUE,
                        plotOptimum = FALSE,
                        labels = "numb",
                        addTriangles = TRUE,
                        addHull = TRUE)
{
  plotPolytope(A, b, type = type, crit = crit, faces = faces, plotFaces = plotFaces,
               plotFeasible = plotFeasible, plotOptimum = plotOptimum, labels = labels)
}

```

```

plotCriterion2D(A, b, obj, type = type, crit = crit, addTriangles = addTriangles,
               addHull = addHull, plotFeasible = plotFeasible, labels = labels)
}

### Bi-objective problem with three variables
loadView <- function(fname = "view.RData", v = NULL) {
  if (!is.null(v)) {
    rgl::view3d(userMatrix = v)
  } else {
    if (file.exists(fname)) {
      load(fname)
      rgl::view3d(userMatrix = view)
    } else {
      warning(paste0("Can't TRUE load view in file ", fname, "!"))
    }
  }
}

## Ex
view <- matrix( c(-0.452365815639496, -0.446501553058624, 0.77201122045517, 0, 0.886364221572876,
                 -0.320795893669128, 0.333835482597351, 0, 0.0986008867621422, 0.835299551486969,
                 0.540881276130676, 0, 0, 0, 0, 1), nc = 4)
loadView(v = view)
Ab <- matrix( c(
  1, 1, 2, 5,
  2, -1, 0, 3,
  -1, 2, 1, 3,
  0, -3, 5, 2
), nc = 4, byrow = TRUE)
A <- Ab[,1:3]
b <- Ab[,4]
obj <- matrix(c(1, -6, 3, -4, 1, 6), nrow = 2)

# LP model
plotBiObj3D(A, b, obj, crit = "min", addTriangles = FALSE)

# ILP model
plotBiObj3D(A, b, obj, type = c("i","i","i"), crit = "min")

# MILP model
plotBiObj3D(A, b, obj, type = c("c","i","i"), crit = "min")
plotBiObj3D(A, b, obj, type = c("i","c","i"), crit = "min")
plotBiObj3D(A, b, obj, type = c("i","i","c"), crit = "min")
plotBiObj3D(A, b, obj, type = c("i","c","c"), crit = "min")
plotBiObj3D(A, b, obj, type = c("c","i","c"), crit = "min")
plotBiObj3D(A, b, obj, type = c("c","c","i"), crit = "min")

## Ex
view <- matrix( c(0.976349174976349, -0.202332556247711, 0.0761845782399178, 0, 0.0903248339891434,
                 0.701892614364624, 0.706531345844269, 0, -0.196427255868912, -0.682940244674683,
                 0.703568696975708, 0, 0, 0, 0, 1), nc = 4)
loadView(v = view)

```

```

A <- matrix( c(
  -1, 1, 0,
  1, 4, 0,
  2, 1, 0,
  3, -4, 0,
  0, 0, 4
), nc = 3, byrow = TRUE)
b <- c(5, 45, 27, 24, 10)
obj <- matrix(c(1, -6, 3, -4, 1, 6), nrow = 2)

# LP model
plotBiObj3D(A, b, obj, crit = "min", addTriangles = FALSE, labels = "coord")

# ILP model
plotBiObj3D(A, b, obj, type = c("i","i","i"))

# MILP model
plotBiObj3D(A, b, obj, type = c("c","i","i"))
plotBiObj3D(A, b, obj, type = c("i","c","i"), plotFaces = FALSE)
plotBiObj3D(A, b, obj, type = c("i","i","c"))
plotBiObj3D(A, b, obj, type = c("i","c","c"), plotFaces = FALSE)
plotBiObj3D(A, b, obj, type = c("c","i","c"), plotFaces = FALSE)
plotBiObj3D(A, b, obj, type = c("c","c","i"))

## Ex
view <- matrix( c(-0.812462985515594, -0.029454167932272, 0.582268416881561, 0, 0.579295456409454,
  -0.153386667370796, 0.800555109977722, 0, 0.0657325685024261, 0.987727105617523,
  0.14168381690979, 0, 0, 0, 0, 1), nc = 4)
loadView(v = view)
A <- matrix( c(
  1, 1, 1,
  3, 0, 1
), nc = 3, byrow = TRUE)
b <- c(10, 24)
obj <- matrix(c(1, -6, 3, -4, 1, 6), nrow = 2)

# LP model
plotBiObj3D(A, b, obj, crit = "min", addTriangles = FALSE, labels = "coord")

# ILP model
plotBiObj3D(A, b, obj, type = c("i","i","i"), crit = "min", labels = "n")

# MILP model
plotBiObj3D(A, b, obj, type = c("c","i","i"), crit = "min")
plotBiObj3D(A, b, obj, type = c("i","c","i"), crit = "min")
plotBiObj3D(A, b, obj, type = c("i","i","c"), crit = "min")
plotBiObj3D(A, b, obj, type = c("i","c","c"), crit = "min")
plotBiObj3D(A, b, obj, type = c("c","i","c"), crit = "min", plotFaces = FALSE)
plotBiObj3D(A, b, obj, type = c("c","c","i"), crit = "min", plotFaces = FALSE)

## Ex

```

```

view <- matrix( c(-0.412063330411911, -0.228006735444069, 0.882166087627411, 0, 0.910147845745087,
                 -0.0574885793030262, 0.410274744033813, 0, -0.042830865830183, 0.97196090221405,
                 0.231208890676498, 0, 0, 0, 0, 1), nc = 4)

loadView(v = view)
A <- matrix( c(
3, 2, 5,
2, 1, 1,
1, 1, 3,
5, 2, 4
), nc = 3, byrow = TRUE)
b <- c(55, 26, 30, 57)
obj <- matrix(c(1, -6, 3, -4, 1, -1), nrow = 2)

# LP model
plotBiObj3D(A, b, obj, crit = "min", addTriangles = FALSE, labels = "coord")

# ILP model
plotBiObj3D(A, b, obj, type = c("i","i","i"), crit = "min", labels = "n")

# MILP model
plotBiObj3D(A, b, obj, type = c("c","i","i"), crit = "min", labels = "n")
plotBiObj3D(A, b, obj, type = c("i","c","i"), crit = "min", labels = "n", plotFaces = FALSE)
plotBiObj3D(A, b, obj, type = c("i","i","c"), crit = "min", labels = "n")
plotBiObj3D(A, b, obj, type = c("i","c","c"), crit = "min", labels = "n")
plotBiObj3D(A, b, obj, type = c("c","i","c"), crit = "min", labels = "n", plotFaces = FALSE)
plotBiObj3D(A, b, obj, type = c("c","c","i"), crit = "min", labels = "n")

```

---

plotPolytope

*Plot the polytope (bounded convex set) of a linear mathematical program*


---

## Description

Plot the polytope (bounded convex set) of a linear mathematical program

## Usage

```

plotPolytope(A, b, obj = NULL, type = rep("c", ncol(A)),
  nonneg = rep(TRUE, ncol(A)), crit = "max", faces = type,
  plotFaces = TRUE, plotFeasible = TRUE, plotOptimum = FALSE,
  latex = FALSE, labels = NULL, ...)

```

## Arguments

A	The constraint matrix.
b	Right hand side.
obj	A vector with objective coefficients.

type	A character vector of same length as number of variables. If entry $k$ is 'i' variable $k$ must be integer and if 'c' continuous.
nonneg	A boolean vector of same length as number of variables. If entry $k$ is TRUE then variable $k$ must be non-negative.
crit	Either max or min (only used if add the iso profit line)
faces	A character vector of same length as number of variables. If entry $k$ is 'i' variable $k$ must be integer and if 'c' continuous. Useful if e.g. want to show the linear relaxation of an IP.
plotFaces	If True then plot the faces.
plotFeasible	If True then plot the feasible points/segments (relevant for IPLP/MILP).
plotOptimum	Show the optimum corner solution point (if alternative solutions only one is shown) and add the iso profit line.
latex	If True make latex math labels for TikZ.
labels	If NULL don't add any labels. If 'n' no labels but show the points. If 'coord' add coordinates to the points. Otherwise number all points from one.
...	If 2D arguments passed to the <code>aes_string</code> function in <code>geom_point</code> or <code>geom_line</code> .

**Value**

If 2D a ggplot2 object. If 3D a rgl window with 3D plot.

**Note**

The feasible region defined by the constraints must be bounded otherwise you may see strange results.

**Author(s)**

Lars Relund <lars@relund.dk>

**Examples**

```
### 2D examples
# Define the model max/min coeff*x st. Ax<=b, x>=0
A <- matrix(c(-3,2,2,4,9,10), ncol = 2, byrow = TRUE)
b <- c(3,27,90)
obj <- c(7.75, 10)

## LP model
# The polytope with the corner points
plotPolytope(
  A,
  b,
  obj,
  type = rep("c", ncol(A)),
  crit = "max",
  faces = rep("c", ncol(A)),
  plotFaces = TRUE,
```

```

    plotFeasible = TRUE,
    plotOptimum = FALSE,
    labels = NULL
  )
  # With optimum and labels:
  plotPolytope(
    A,
    b,
    obj,
    type = rep("c", ncol(A)),
    crit = "max",
    faces = rep("c", ncol(A)),
    plotFaces = TRUE,
    plotFeasible = TRUE,
    plotOptimum = TRUE,
    labels = "coord"
  )
  # Minimize:
  plotPolytope(
    A,
    b,
    obj,
    type = rep("c", ncol(A)),
    crit = "min",
    faces = rep("c", ncol(A)),
    plotFaces = TRUE,
    plotFeasible = TRUE,
    plotOptimum = TRUE,
    labels = "n"
  )
  # Note return a ggplot so can e.g. add other labels on e.g. the axes:
  p <- plotPolytope(
    A,
    b,
    obj,
    type = rep("c", ncol(A)),
    crit = "max",
    faces = rep("c", ncol(A)),
    plotFaces = TRUE,
    plotFeasible = TRUE,
    plotOptimum = TRUE,
    labels = "coord"
  )
  p + ggplot2::xlab("x") + ggplot2::ylab("y")

# More examples

## LP-model with no non-negativity constraints
A <- matrix(c(-3, 2, 2, 4, 9, 10, 1, -2), ncol = 2, byrow = TRUE)
b <- c(3, 27, 90, 2)
obj <- c(7.75, 10)
plotPolytope(
  A,

```



```

    b,
    obj,
    type = rep("c", ncol(A)),
    nonneg = rep(FALSE, ncol(A)),
    crit = "max",
    faces = rep("c", ncol(A)),
    plotFaces = TRUE,
    plotFeasible = TRUE,
    plotOptimum = FALSE,
    labels = NULL
  )

```

## The package don't plot feasible regions that are unbounded e.g if we drop the 2 and 3 constraint

```
A <- matrix(c(-3,2), ncol = 2, byrow = TRUE)
```

```
b <- c(3)
```

```
obj <- c(7.75, 10)
```

```
# Wrong plot
```

```
plotPolytope(
  A,
  b,
  obj,
  type = rep("c", ncol(A)),
  crit = "max",
  faces = rep("c", ncol(A)),
  plotFaces = TRUE,
  plotFeasible = TRUE,
  plotOptimum = FALSE,
  labels = NULL
)

```

# One solution is to add a bounding box and check if the bounding box is binding

```
A <- rbind(A, c(1,0), c(0,1))
```

```
b <- c(b, 10, 10)
```

```
plotPolytope(
  A,
  b,
  obj,
  type = rep("c", ncol(A)),
  crit = "max",
  faces = rep("c", ncol(A)),
  plotFaces = TRUE,
  plotFeasible = TRUE,
  plotOptimum = FALSE,
  labels = NULL
)

```

## ILP model

```
A <- matrix(c(-3,2,2,4,9,10), ncol = 2, byrow = TRUE)
```

```
b <- c(3,27,90)
```

```
obj <- c(7.75, 10)
```

```
# ILP model with LP faces:
```

```

plotPolytope(
  A,
  b,
  obj,
  type = rep("i", ncol(A)),
  crit = "max",
  faces = rep("c", ncol(A)),
  plotFaces = TRUE,
  plotFeasible = TRUE,
  plotOptimum = TRUE,
  labels = "coord"
)
#ILP model with IP faces:
plotPolytope(
  A,
  b,
  obj,
  type = rep("i", ncol(A)),
  crit = "max",
  faces = rep("i", ncol(A)),
  plotFaces = TRUE,
  plotFeasible = TRUE,
  plotOptimum = TRUE,
  labels = "coord"
)

## MILP model
A <- matrix(c(-3,2,2,2,4,9,10), ncol = 2, byrow = TRUE)
b <- c(3,27,90)
obj <- c(7.75, 10)
# Second coordinate integer
plotPolytope(
  A,
  b,
  obj,
  type = c("c", "i"),
  crit = "max",
  faces = c("c", "i"),
  plotFaces = FALSE,
  plotFeasible = TRUE,
  plotOptimum = TRUE,
  labels = "coord"
)
# First coordinate integer and with LP faces:
plotPolytope(
  A,
  b,
  obj,
  type = c("i", "c"),
  crit = "max",
  faces = c("c", "c"),
  plotFaces = TRUE,

```

```

    plotFeasible = TRUE,
    plotOptimum = TRUE,
    labels = "coord"
  )
# First coordinate integer and with LP faces:
plotPolytope(
  A,
  b,
  obj,
  type = c("i", "c"),
  crit = "max",
  faces = c("i", "c"),
  plotFaces = TRUE,
  plotFeasible = TRUE,
  plotOptimum = TRUE,
  labels = "coord"
)

### 3D examples
# Ex 1
view <- matrix( c(-0.412063330411911, -0.228006735444069, 0.882166087627411, 0, 0.910147845745087,
                 -0.0574885793030262, 0.410274744033813, 0, -0.042830865830183, 0.97196090221405,
                 0.231208890676498, 0, 0, 0, 0, 1), nc = 4)

loadView(v = view)
A <- matrix( c(
  3, 2, 5,
  2, 1, 1,
  1, 1, 3,
  5, 2, 4
), nc = 3, byrow = TRUE)
b <- c(55, 26, 30, 57)
obj <- c(20, 10, 15)
# LP model
plotPolytope(A, b, plotOptimum = TRUE, obj = obj, labels = "coord")
# ILP model
plotPolytope(A, b, faces = c("c", "c", "c"), type = c("i", "i", "i"), plotOptimum = TRUE, obj = obj)
# MILP model
plotPolytope(A, b, faces = c("c", "c", "c"), type = c("i", "c", "i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c", "c", "c"), type = c("c", "i", "i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c", "c", "c"), type = c("i", "i", "c"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c", "c", "c"), type = c("i", "i", "c"), plotFaces = FALSE)
plotPolytope(A, b, type = c("i", "c", "c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c", "i", "c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c", "c", "i"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)

# Ex 2
view <- matrix( c(-0.812462985515594, -0.029454167932272, 0.582268416881561, 0, 0.579295456409454,
                 -0.153386667370796, 0.800555109977722, 0, 0.0657325685024261, 0.987727105617523,
                 0.14168381690979, 0, 0, 0, 0, 1), nc = 4)

loadView(v = view)

```

```

A <- matrix( c(
  1, 1, 1,
  3, 0, 1
), nc = 3, byrow = TRUE)
b <- c(10, 24)
obj <- c(20, 10, 15)
plotPolytope(A, b, plotOptimum = TRUE, obj = obj, labels = "coord")
# ILP model
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","i"), plotOptimum = TRUE, obj = obj)
# MILP model
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","c","i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("c","i","i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","c"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","c"), plotFaces = FALSE)
plotPolytope(A, b, type = c("i","c","c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c","i","c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c","c","i"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)

# Ex 3
view <- matrix( c(0.976349174976349, -0.202332556247711, 0.0761845782399178, 0, 0.0903248339891434,
  0.701892614364624, 0.706531345844269, 0, -0.196427255868912, -0.682940244674683,
  0.703568696975708, 0, 0, 0, 0, 1), nc = 4)
loadView(v = view)
A <- matrix( c(
  -1, 1, 0,
  1, 4, 0,
  2, 1, 0,
  3, -4, 0,
  0, 0, 4
), nc = 3, byrow = TRUE)
b <- c(5, 45, 27, 24, 10)
obj <- c(5, 45, 15)
plotPolytope(A, b, plotOptimum = TRUE, obj = obj, labels = "coord")
# ILP model
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","i"), plotOptimum = TRUE, obj = obj)
# MILP model
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","c","i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("c","i","i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","c"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","c"), plotFaces = FALSE)
plotPolytope(A, b, type = c("i","c","c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c","i","c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c","c","i"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)

# Ex 4
view <- matrix( c(-0.452365815639496, -0.446501553058624, 0.77201122045517, 0, 0.886364221572876,
  -0.320795893669128, 0.333835482597351, 0, 0.0986008867621422, 0.835299551486969,
  0.540881276130676, 0, 0, 0, 0, 1), nc = 4)
loadView(v = view)
Ab <- matrix( c(
  1, 1, 2, 5,
  2, -1, 0, 3,
  -1, 2, 1, 3,

```

```

    0, -3, 5, 2
    # 0, 1, 0, 4,
    # 1, 0, 0, 4
), nc = 4, byrow = TRUE)
A <- Ab[,1:3]
b <- Ab[,4]
obj = c(1,1,3)
plotPolytope(A, b, plotOptimum = TRUE, obj = obj, labels = "coord")
# ILP model
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","i"), plotOptimum = TRUE, obj = obj)
# MILP model
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","c","i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("c","i","i"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","c"), plotOptimum = TRUE, obj = obj)
plotPolytope(A, b, faces = c("c","c","c"), type = c("i","i","c"), plotFaces = FALSE)
plotPolytope(A, b, type = c("i","c","c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, type = c("c","i","c"), plotOptimum = TRUE, obj = obj, plotFaces = FALSE)
plotPolytope(A, b, faces = c("c","c","c"), type = c("c","c","i"), plotOptimum = TRUE, obj = obj)

```

---

plotPolytope2D	<i>Plot the polytope (bounded convex set) of a linear mathematical program</i>
----------------	--

---

## Description

Plot the polytope (bounded convex set) of a linear mathematical program

## Usage

```

plotPolytope2D(A, b, obj = NULL, type = rep("c", ncol(A)),
  nonneg = rep(TRUE, ncol(A)), crit = "max", faces = rep("c",
  ncol(A)), plotFaces = TRUE, plotFeasible = TRUE,
  plotOptimum = FALSE, latex = FALSE, labels = NULL, ...)

```

## Arguments

A	The constraint matrix.
b	Right hand side.
obj	A vector with objective coefficients.
type	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.
crit	Either max or min (only used if add the iso profit line)
faces	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous. Useful if e.g. want to show the linear relaxation of an IP.

plotFaces	If True then plot the faces.
plotFeasible	If True then plot the feasible points/segments (relevant for ILP/MILP).
plotOptimum	Show the optimum corner solution point (if alternative solutions only one is shown) and add the iso profit line.
latex	If True make latex math labels for TikZ.
labels	If NULL don't add any labels. If 'n' no labels but show the points. If 'coord' add coordinates to the points. Otherwise number all points from one.
...	If 2D arguments passed to the <a href="#">aes_string</a> function in <a href="#">geom_point</a> or <a href="#">geom_line</a> .

**Value**

A ggplot2 object.

**Author(s)**

Lars Relund <lars@relund.dk>

---

plotPolytope3D	<i>Plot the polytope (bounded convex set) of a linear mathematical program</i>
----------------	--

---

**Description**

Plot the polytope (bounded convex set) of a linear mathematical program

**Usage**

```
plotPolytope3D(A, b, obj = NULL, type = rep("c", ncol(A)),
  nonneg = rep(TRUE, ncol(A)), crit = "max", faces = rep("c",
  ncol(A)), plotFaces = TRUE, plotFeasible = TRUE,
  plotOptimum = FALSE, latex = FALSE, labels = NULL, ...)
```

**Arguments**

A	The constraint matrix.
b	Right hand side.
obj	A vector with objective coefficients.
type	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.
crit	Either max or min (only used if add the iso profit line)
faces	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous. Useful if e.g. want to show the linear relaxation of an IP.

plotFaces	If True then plot the faces.
plotFeasible	If True then plot the feasible points/segments (relevant for IPLP/MILP).
plotOptimum	Show the optimum corner solution point (if alternative solutions only one is shown) and add the iso profit line.
latex	If True make latex math labels for TikZ.
labels	If NULL don't add any labels. If 'n' no labels but show the points. If 'coord' add coordinates to the points. Otherwise number all points from one.
...	Arguments passed to axes3d, plot3d, title3d. Parsed using lists argsAxes3d, argsPlot3d and argsTitle3d.

**Value**

A rgl window with 3D plot.

**Note**

The feasible region defined by the constraints must be bounded otherwise you may see strange results.

**Author(s)**

Lars Relund <lars@relund.dk>

---

 saveView

*Help function to save the view angle for the RGL 3D plot*

---

**Description**

Help function to save the view angle for the RGL 3D plot

**Usage**

```
saveView(fname = "view.RData", overwrite = FALSE, print = FALSE)
```

**Arguments**

fname	The file name of the view.
overwrite	Overwrite existing file.
print	Print the view so can be copied to R code (no file is saved).

**Value**

The ggplot2 object.

**Note**

Only save if the file name don't exists.

**Author(s)**

Lars Relund <lars@relund.dk>

**Examples**

```
view <- matrix( c(-0.412063330411911, -0.228006735444069, 0.882166087627411, 0,
0.910147845745087, -0.0574885793030262, 0.410274744033813, 0, -0.042830865830183,
0.97196090221405, 0.231208890676498, 0, 0, 0, 0, 1), nc = 4)

loadView(v = view)
A <- matrix( c(3, 2, 5, 2, 1, 1, 1, 1, 3, 5, 2, 4), nc = 3, byrow = TRUE)
b <- c(55, 26, 30, 57)
obj <- c(20, 10, 15)
plotPolytope(A, b, plotOptimum = TRUE, obj = obj, labels = "coord")

# Try to modify the angle in the RGL window
saveView(print = TRUE) # get the viewangle to insert into R code
```

---

slices

*Find all corner points in the slices define for each fixed integer combination.*

---

**Description**

Find all corner points in the slices define for each fixed integer combination.

**Usage**

```
slices(A, b, type = rep("c", ncol(A)), nonneg = rep(TRUE, ncol(A)),
collapse = FALSE)
```

**Arguments**

A	The constraint matrix.
b	Right hand side.
type	A character vector of same length as number of variables. If entry k is 'i' variable k must be integer and if 'c' continuous.
nonneg	A boolean vector of same length as number of variables. If entry k is TRUE then variable k must be non-negative.
collapse	Collapse list to a data frame with unique points.

**Value**

A list with the corner points (one entry for each slice).



**Examples**

```
A <- matrix( c(3, -2, 1,2, 4, -2,-3, 2, 1), nc = 3, byrow = TRUE)
b <- c(10,12,3)
slices(A, b, type=c("i","c","i"))
```

```
A <- matrix(c(9,10,2,4,-3,2), ncol = 2, byrow = TRUE)
b <- c(90,27,3)
slices(A, b, type=c("c","i"), collapse = TRUE)
```

# Index

\*Topic **package**

gMOIP, 5

aes\_string, 15, 22

clear3d, 8

cornerPoints, 2

cornerPointsCont, 3

criterionPoints, 3

df2String, 4

geom\_line, 15, 22

geom\_point, 15, 22

gMOIP, 5

gMOIP-package (gMOIP), 5

hullSegment, 5

inHull, 6

integerPoints, 7

loadView, 8

mergeLists, 9

plotCriterion2D, 5, 9

plotPolytope, 5, 14

plotPolytope2D, 21

plotPolytope3D, 22

rgl.close, 8

saveView, 23

slices, 24

view3d, 8