

Package ‘NNLM’

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Type Package

Title Fast and Versatile Non-Negative Matrix Factorization

Description This is a package for Non-Negative Linear Models (NNLM). It implements fast sequential coordinate descent algorithms for non-negative linear regression and non-negative matrix factorization (NMF). It supports mean square error and Kullback-Leibler divergence loss. Many other features are also implemented, including missing value imputation, domain knowledge integration, designable W and H matrices and multiple forms of regularizations.

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BugReports <https://github.com/linxihui/NNLM/issues>

URL <https://github.com/linxihui/NNLM>

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mse.mkl	<i>Compute mean square error(MSE) and mean kL divergence (MKL)</i>
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Description

Compute mean square error(MSE) and mean kL divergence (MKL)

Usage

```
mse.mkl(obs, pred, na.rm = TRUE, show.warning = TRUE)
```

Arguments

obs	observed value
pred	prediction/estimate
na.rm	if to remove NAs
show.warning	if to show warning if any

Value

A vector of c(MSE, MKL)

nnlm	<i>Non-negative linear model/regression (NNLM)</i>
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Description

Solving non-negative linear regression problem as

$$\operatorname{argmin}_{\beta \geq 0} L(y - x\beta) + \alpha_1 \|\beta\|_2^2 + \alpha_2 \sum_{i < j} \beta_i^T \beta_j^T + \alpha_3 \|\beta\|_1$$

where L is a loss function of either square error or Kullback-Leibler divergence.

Usage

```
nnlm(x, y, alpha = rep(0, 3), method = c("scd", "lee"),
     loss = c("mse", "mkl"), init = NULL, mask = NULL, check.x = TRUE,
     max.iter = 10000L, rel.tol = 1e-12, n.threads = 1L,
     show.warning = TRUE)
```

Arguments

<code>x</code>	Design matrix
<code>y</code>	Vector or matrix of response
<code>alpha</code>	A vector of non-negative value length equal to or less than 3, meaning [L2, angle, L1] regularization on beta (non-masked entries)
<code>method</code>	Iteration algorithm, either 'scd' for sequential coordinate-wise descent or 'lee' for Lee's multiplicative algorithm
<code>loss</code>	Loss function to use, either 'mse' for mean square error or 'mkl' for mean KL-divergence. Note that if <code>x</code> , <code>y</code> contains negative values, one should always use 'mse'
<code>init</code>	Initial value of beta for iteration. Either NULL (default) or a non-negative matrix of
<code>mask</code>	Either NULL (default) or a logical matrix of the same shape as beta, indicating if an entry should be fixed to its initial (if <code>init</code> specified) or 0 (if <code>init</code> not specified).
<code>check.x</code>	If to check the condition number of <code>x</code> to ensure unique solution. Default to TRUE but could be slow
<code>max.iter</code>	Maximum number of iterations
<code>rel.tol</code>	Stop criterion, relative change on <code>x</code> between two successive iteration. It is equal to $2 * e2 - e1 / (e2 + e1)$. One could specify a negative number to force an exact <code>max.iter</code> iteration, i.e., not early stop
<code>n.threads</code>	An integer number of threads/CPU's to use. Default to 1 (no parallel). Use 0 or a negative value for all cores
<code>show.warning</code>	If to shown warnings if exists. Default to TRUE

Details

The linear model is solve in column-by-column manner, which is paralleled. When $y_{.j}$ (j -th column) contains missing values, only the complete entries are used to solve $\beta_{.j}$. Therefore, the minimum complete entries of each column should be not smaller than number of columns of `x` when penalty is not used.

`method = 'scd'` is recommended, especially when the solution is probably sparse. Though both "mse" and "mkl" loss are supported for non-negative `x` and `y`, only "mse" is proper when either `y` or `x` contains negative value. Note that loss "mkl" is much slower then loss "mse", which might be your concern when `x` and `y` is extremely large.

`mask` is can be used for hard regularization, i.e., forcing entries to their initial values (if `init` specified) or 0 (if `init` not specified). Internally, `mask` is achieved by skipping the masked entries during the element-wise iteration.

Value

An object of class 'nnlm', which is a list with components

- coefficients : a matrix or vector (depend on y) of the NNLM solution, i.e., β
- n.iteration : total number of iteration (sum over all column of beta)
- error : a vector of errors/loss as c(MSE, MKL, target.error) of the solution
- options : list of information of input arguments
- call : function call

Author(s)

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References

Franc, V. C., Hlavac, V. C., Navara, M. (2005). Sequential Coordinate-Wise Algorithm for the Non-negative Least Squares Problem. Proc. Int'l Conf. Computer Analysis of Images and Patterns. Lecture Notes in Computer Science 3691. p. 407.

Lee, Daniel D., and H. Sebastian Seung. 1999. "Learning the Parts of Objects by Non-Negative Matrix Factorization." Nature 401: 788-91.

Pascual-Montano, Alberto, J.M. Carazo, Kieko Kochi, Dietrich Lehmann, and Roberto D.Pascual-Marqui. 2006. "Nonsmooth Nonnegative Matrix Factorization (NsNMF)." IEEE Transactions on Pattern Analysis and Machine Intelligence 28 (3): 403-14.

Examples

```
# without negative value
x <- matrix(runif(50*20), 50, 20);
beta <- matrix(rexp(20*2), 20, 2);
y <- x %*% beta + 0.1*matrix(runif(50*2), 50, 2);
beta.hat <- nnlm(x, y, loss = 'mkl');

# with negative values
x2 <- 10*matrix(rnorm(50*20), 50, 20);
y2 <- x2 %*% beta + 0.2*matrix(rnorm(50*2), 50, 2);
beta.hat2 <- nnlm(x, y);
```

 nnmf

Non-negative matrix factorization

Description

Non-negative matrix factorization(NMF or NNMF) using sequential coordinate-wise descent or multiplicative updates

Usage

```
nmf(A, k = 1L, alpha = rep(0, 3), beta = rep(0, 3),
    method = c("scd", "lee"), loss = c("mse", "mkl"), init = NULL,
    mask = NULL, W.norm = -1L, check.k = TRUE, max.iter = 500L,
    rel.tol = 1e-04, n.threads = 1L, trace = 100/inner.max.iter,
    verbose = 1L, show.warning = TRUE, inner.max.iter = ifelse("mse" ==
    loss, 50L, 1L), inner.rel.tol = 1e-09)
```

Arguments

A	A matrix to be decomposed
k	An integer of decomposition rank
alpha	[L2, angle, L1] regularization on W (non-masked entries)
beta	[L2, angle, L1] regularization on H (non-masked entries)
method	Decomposition algorithms, either 'scd' for sequential coordinate-wise descent(default) or 'lee' for Lee's multiplicative algorithm
loss	Loss function to use, either 'mse' for mean square error (default) or 'mkl' for mean KL-divergence
init	A list of initial matrices for W and H. One can also supply known matrices W0, H0, and initialize their correspondent matrices H1 and W1. See details
mask	A list of mask matrices for W, H, H1 (if init\$W0 supplied), W1 (if init\$H0 supplied), which should have the same shapes as W, H, H1 and W1 if specified. If initial matrices not specified, masked entries are fixed to 0. See details
W.norm	A numeric value 'p' indicating the L_p -norm (can be infinity) used to normalized the outcome W matrix. No normalization will be performed if 0 or negative. This argument has no effect on outcome correspondent to known profiles W0, H0. Default to 1, i.e. sum of W should sum up to 1, which can be interpreted as "distribution" or "proportion"
check.k	If to check whether $k \leq nm/(n+m)$, where (n,m)=dim(A), or k is smaller than the column-wise and row-wise minimum numbers of complete observation
max.iter	Maximum iteration of alternating NNLS solutions to H and W
rel.tol	Stop criterion, which is relative tolerance between two successive iterations, = $le2-e1/avg(e1, e2)$
n.threads	An integer number of threads/CPU's to use. Default to 1(no parallel). Specify 0 for all cores
trace	An integer indicating how frequent the error should be checked. MSE and MKL error will computed every trace iterations. If 0 or negative, trace is set to a very large number and only errors of the first and last iterations are checked.
verbose	Either 0/FALSE, 1/TRUE or 2, with 0/FALSE/else = no any tracking, 1 == progression bar, 2 == print iteration info.
show.warning	If to show warnings when targeted rel.tol is not reached
inner.max.iter	Maximum number of iterations passed to each inner W or H matrix updating loop
inner.rel.tol	Stop criterion for the inner loop, which is relative tolerance passed to inner W or H matrix updating i.e., $le2-e1/avg(e1, e2)$

Details

The problem of non-negative matrix factorization is to find W, H, W_1, H_1 , such that

$$A = WH + W_0H_1 + W_1H_0 + \varepsilon = [WW_0W_1][H'H_1H_0]' + \varepsilon$$

where W_0, H_0 are known matrices, which are NULLs in most application case and ε is noise.. In tumor content deconvolution, W_0 can be thought as known healthy profile, and W is desired pure cancer profile. One also set H_0 to a row matrix of 1, and thus W_1 can be treated as common profile among samples. Use `init` to specify W_0 and H_0 .

Argument `init`, if used, must be a list with entries named as 'W', 'H', 'W0', 'W1', 'H1', 'H0'. One could specify only a few of them. Only use 'W0' (and its correspondent 'H1') or 'H0' (and its correspondent 'W1') for known matrices/profiles.

Similarly, argument `mask`, if used, must be a list entries named as 'W', 'H', 'W0', 'W1', 'H1', 'H0', and they should be either NULL (no specified) or a logical matrix. If a masked for matrix is specified, then masked entries will be fixed to their initial values if initialized (skipped during iteration), or 0 if not initialized.

To simplify the notations, we denote right hand side of the above equation as WH . The problem to solved using square error is

$$\operatorname{argmin}_{W \geq 0, H \geq 0} L(A, WH) + J(W, \alpha) + J(H', \beta)$$

where $L(x, y)$ is a loss function either a square loss

$$\frac{1}{2} \|x - y\|_2^2$$

or a Kullback-Leibler divergence

$$x \log(x/y) - x - y,$$

and

$$J(X, \alpha) = \alpha_1 J_1(X) + \alpha_2 J_2(X) + \alpha_3 J_3(X),$$

$$J_1(X) = \frac{1}{2} \|X\|_F^2 = \frac{1}{2} \operatorname{tr}(XX^T),$$

$$J_2(X) = \sum_{i < j} (X_{.i})^T X_{.j} = \frac{1}{2} \operatorname{tr}(X(E - I)X^T),$$

$$J_3(X) = \sum_{i,j} |x_{ij}| = \operatorname{tr}(XE).$$

The formal one is usually better for symmetric distribution, while the later one is more suitable for skewed distribution, especially for count data as it can be derived from Poisson distributed observation. The penalty function J is a composition of three types of penalties, which aim to minimizing L2 norm, maximizing angles between hidden features (columns of W and rows of H) and L1 norm (sparsity). The parameters α, β of length 3 indicates the amount of penalties.

When `method == 'scd'`, a sequential coordinate-wise descent algorithm is used when solving W and H alternatively, which are non-negative regression problem. The `inner.max.iter` and

`inner.rel.tol` is used to control the number of iteration for these non-negative regressions. This is also applicable to `method == 'lee'` (the original algorithm only iteration through all entries once for each iteration), which is usually faster than the original algorithm when `loss == 'mse'`. When `loss == 'mkl'`, a quadratic approximation to the KL-divergence is used when `method == 'scd'`. Generally, for run time, 'scd' is faster than 'lee' and 'mse' is faster than 'mkl'.

Value

A list with components

- `W` : left matrix, including known `W0` and `W1` if available, i.e., column stacked as $[W, W0, W1]$
- `H` : right matrix, including `H1` and known `H0` if available, i.e. row stacked as $[H', H1', H0']'$
- `mse` : a vector of mean squared errors through iterations
- `mkl` : a vector of mean KL-divergence through iterations
- `target.loss` : target for minimization, which is mean KL-divergence (if `loss == 'mkl'`) or half of mean squared error if `loss == 'mse'` plus penalties
- `average.epochs` : a vector of average epochs (one complete swap over `W` and `H`)
- `n.iteration` : total number of iteration (sum over all column of `beta`)
- `run.time` : running time
- `options` : list of information of input arguments
- `call` : function call

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References

Franc, V. C., Hlavac, V. C., Navara, M. (2005). Sequential Coordinate-Wise Algorithm for the Non-negative Least Squares Problem. Proc. Int'l Conf. Computer Analysis of Images and Patterns. Lecture Notes in Computer Science 3691. p. 407.

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See Also

[nnlm](#), [predict.nnmf](#)

Examples

```

# Pattern extraction, meta-gene
set.seed(123);

data(nsclc, package = 'NNLM')
str(nsclc)

decomp <- nnmf(nsclc[, 1:80], 3, rel.tol = 1e-5);

heatmap(decomp$W, Colv = NA, xlab = 'Meta-gene', ylab = 'Gene', margins = c(2,2),
labRow = '', labCol = '', scale = 'column', col = cm.colors(100));
heatmap(decomp$H, Rowv = NA, ylab = 'Meta-gene', xlab = 'Patient', margins = c(2,2),
labRow = '', labCol = '', scale = 'row', col = cm.colors(100));

# missing value imputation
set.seed(123);
nsclc2 <- nsclc;
index <- sample(length(nsclc2), length(nsclc2)*0.3);
nsclc2[index] <- NA;

# impute using NMF
system.time(nsclc2.nmf <- nnmf(nsclc2, 2));
nsclc2.hat.nmf <- with(nsclc2.nmf, W %*% H);

mse.mkl(nsclc[index], nsclc2.hat.nmf[index])

```

nsclc

Micro-array data of NSCLC patients

Description

This dataset is a random subset (matrix) of micro-array data from a group of Non-Small Cell Lung Cancer (NSCLC) patients. It contains 200 probes / genes (row) for 100 patients / samples (column).

predict.nnmf

Methods for nnmf object returned by nnmf

Description

Methods for nnmf object returned by nnmf

Usage

```
## S3 method for class 'nnmf'  
predict(object, newdata, which = c("A", "W", "H"),  
        method = object$options$method, loss = object$options$loss, ...)  
  
## S3 method for class 'nnmf'  
print(x, ...)
```

Arguments

<code>object</code>	An NNMF object returned by nnmf
<code>newdata</code>	A new matrix of <code>x</code> . No required when <code>which == 'A'</code>
<code>which</code>	Either 'A' (default), 'W' or 'H'
<code>method</code>	Either 'scd' or 'lee'. Default to <code>object\$options\$method</code>
<code>loss</code>	Either 'mse' or 'mkl'. Default to <code>object\$options\$loss</code>
<code>...</code>	Further arguments passed to 'nnlm' or 'print'
<code>x</code>	An NNMF object returned by nnmf

Value

'A' or a class of 'nnlm' for 'predict.nnmf' and no return for 'print'.

See Also

[nnmf](#), [nnlm](#)

Examples

```
x <- matrix(runif(50*20), 50, 20)  
r <- nnmf(x, 2)  
r  
newx <- matrix(runif(50*30), 50, 30)  
pred <- predict(r, newx, 'H')
```

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